

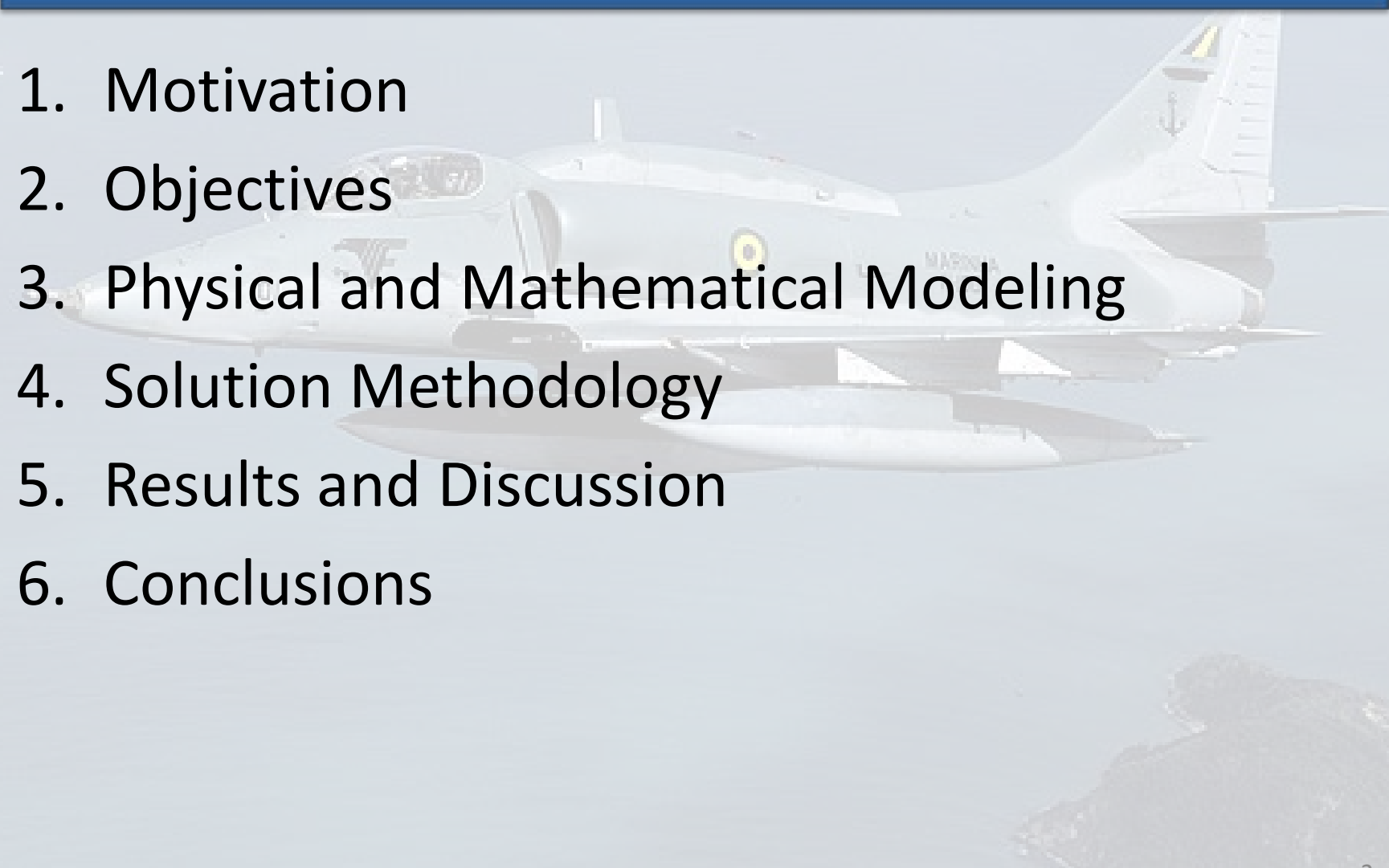


# **Models and Hybrid Solutions for Conjugated Heat Transfer Problems in Aeronautical Airfoils and Sensors**

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# Summary

- 
1. Motivation
  2. Objectives
  3. Physical and Mathematical Modeling
  4. Solution Methodology
  5. Results and Discussion
  6. Conclusions

# 1. Motivation

➤ TsAGI e NASA



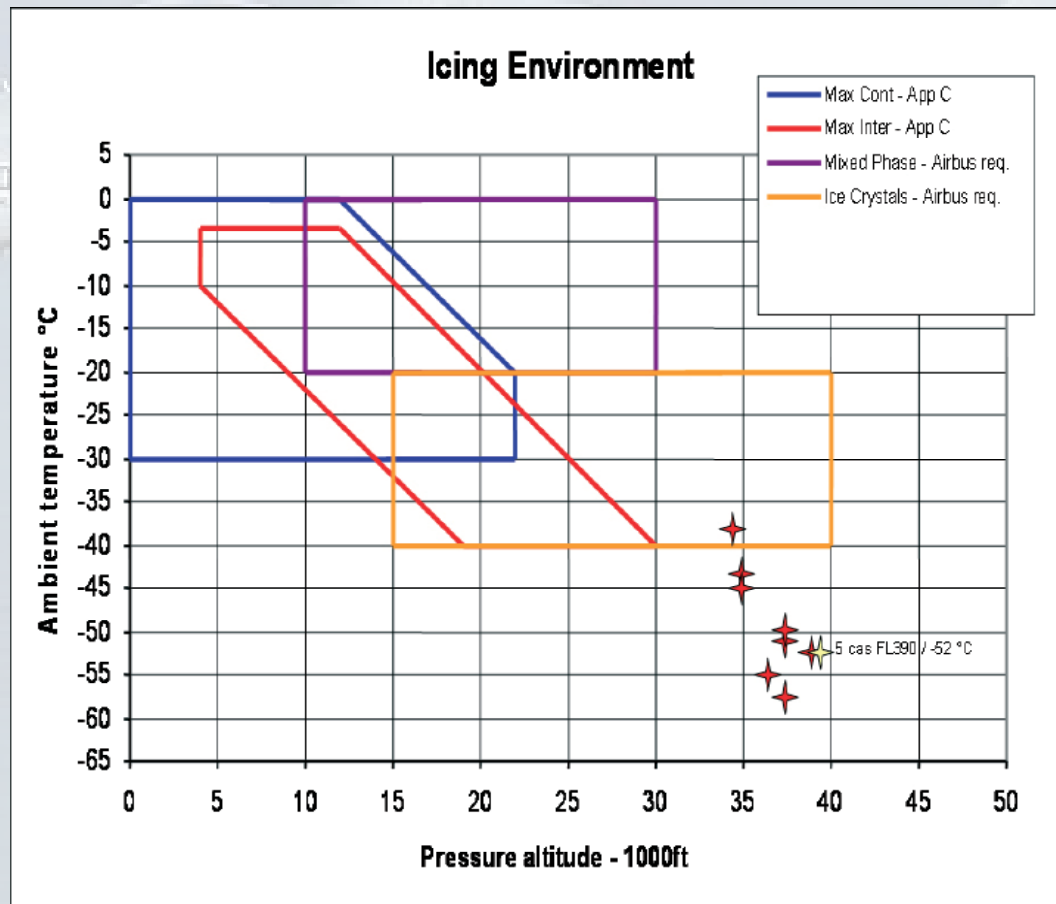
# 1. Motivation

- Accidents involving icing of Pitot probes



# 1. Motivation

## ➤ Certification Envelope and the AFF447 flight



# 1. Motivation

- Aerospace industry moving towards extensive use of composite materials



50% composite by weight



53% composite by weight

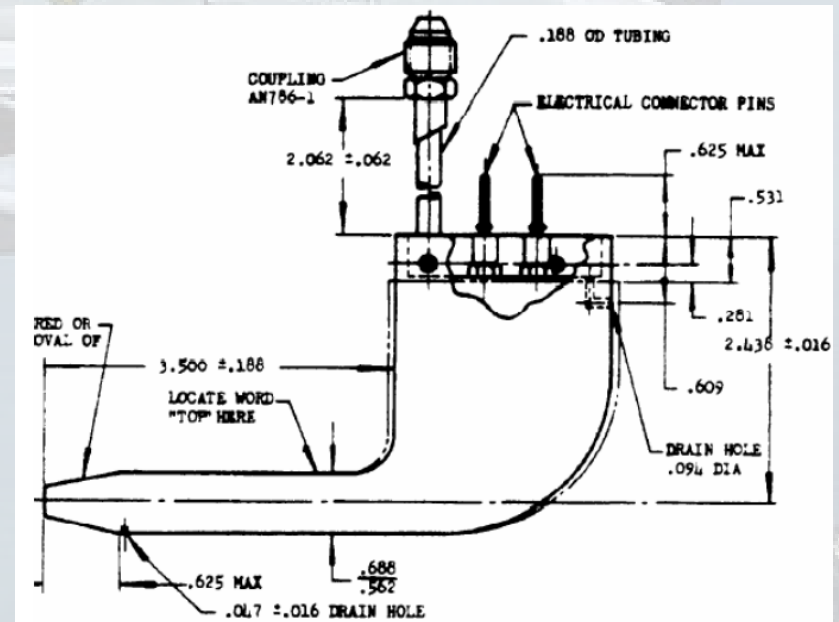
## 2. Objectives

- Show the importance of taking into account the mutual influence between the heat transfer in the solid and in the fluid in icing analysis
- Establish physical and mathematical models for thermal analysis of aeronautical surfaces in the icing wind tunnel
- Physically analyze the thermal behavior of those surfaces and propose design solutions to improve the efficiency of thermal protection systems



# 3. Physical and Mathematical Modeling

- Pitot tube PH-510 manufactured by Aero Instruments, Co., USA





### 3. Physical and Mathematical Modeling

#### ➤ Pitot: Heat Conduction in the Solid

$$w(x) \frac{\partial T_s}{\partial t} = \frac{\partial}{\partial x} \left( k(x) \frac{\partial T_s}{\partial x} \right) + \frac{k(x)}{r} \frac{\partial}{\partial r} \left( r \frac{\partial T_s}{\partial r} \right) + g(x, r, t), 0 \leq x \leq L, r_i(x) \leq r \leq r_o(x)$$

$$T_s(x, r, 0) = T_0(x, r)$$

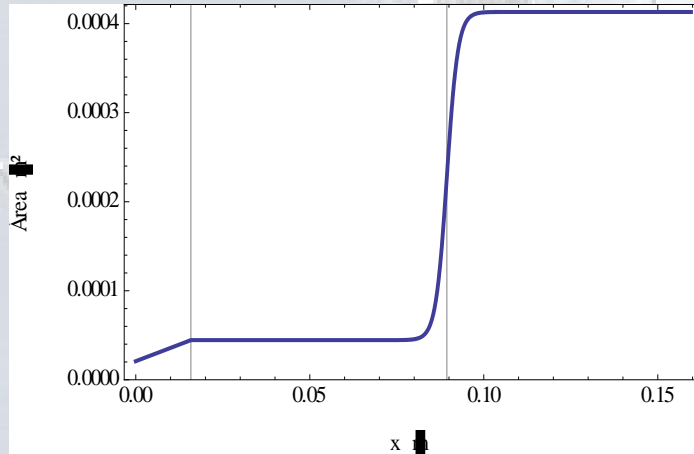
$$h_e T_s(0, r, t) - k(0) \frac{\partial T_s}{\partial x} \Big|_{x=0} = h_e T_{aw}; \quad h_L T_s(L, r, t) + k(L) \frac{\partial T_s}{\partial x} \Big|_{x=L} = h_L T_{aw}$$

$$\frac{\partial T_s}{\partial r} \Big|_{r=r_i(x)} = 0; \quad h(x) T_s(x, r_o(x), t) + k(x) \frac{\partial T_s}{\partial r} \Big|_{r=r_o(x)} = h(x) T_{aw}$$

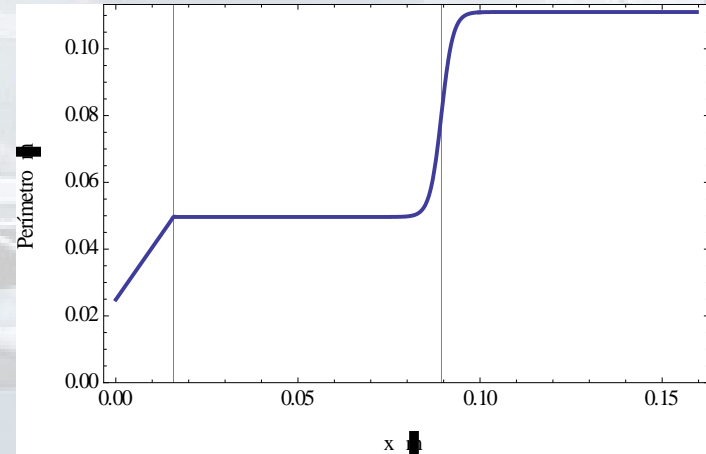
# 3. Physical and Mathematical Modeling

## ➤ Entry Data

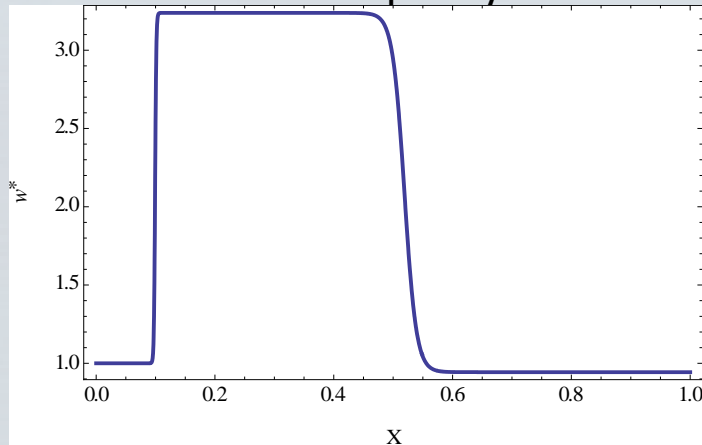
Transversal Section Area



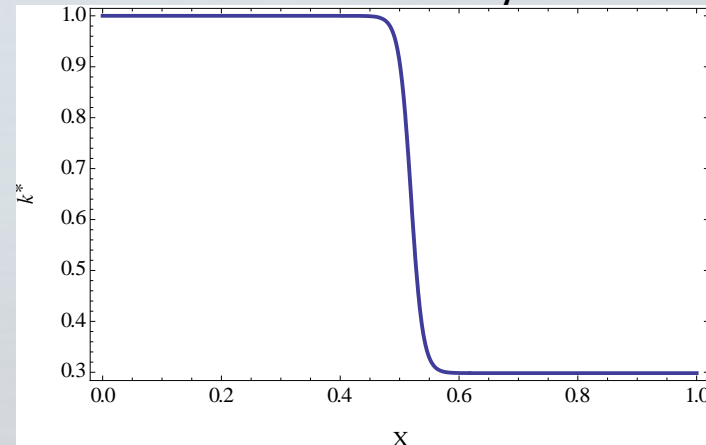
Transversal Section Perimeter



Thermal Capacity

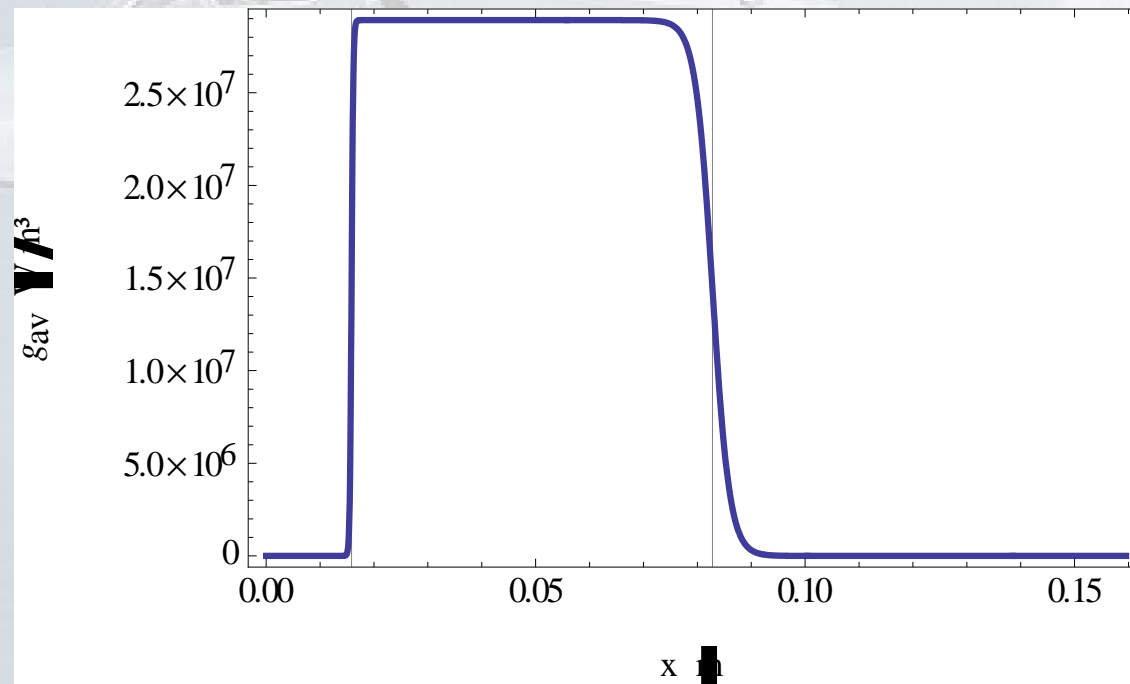


Heat Conductivity



# 3. Physical and Mathematical Modeling

➤ Het generation by Joule Effect



# 3. Physical and Mathematical Modeling

## ➤ Pitot: Boundary Layer Equations

$$\rho u \frac{\partial u}{\partial s} + \bar{\rho} v \frac{\partial u}{\partial y} = \rho_e u_e \frac{du_e}{ds} + \frac{1}{r} \frac{\partial}{\partial y} \left[ (\mu + \mu_t) r \frac{\partial u}{\partial y} \right]$$

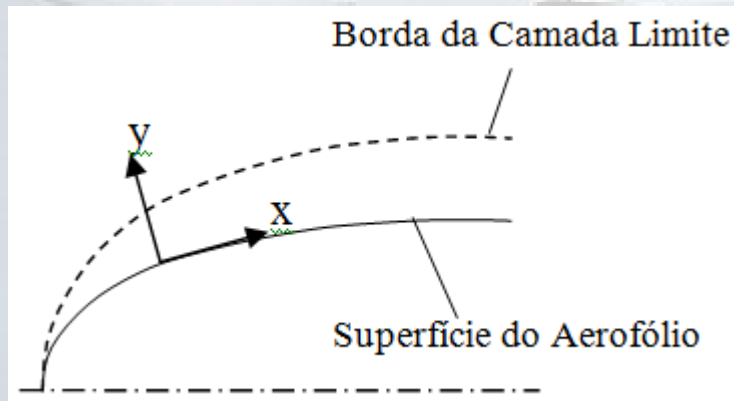
$$u(0) = 0, \quad u(\infty) = u_e, \quad \left. \frac{\partial u}{\partial y} \right|_{y=\infty} = 0$$

$$\rho u \frac{\partial H}{\partial s} + \bar{\rho} v \frac{\partial H}{\partial y} = \frac{1}{r} \frac{\partial}{\partial y} \left[ \left( \frac{\mu}{Pr} + \frac{\mu_t}{Pr_t} \right) r \frac{\partial H}{\partial y} \right] + \frac{1}{r} \frac{\partial}{\partial y} \left[ \mu r \left( 1 - \frac{1}{Pr} \right) + \mu_t r \left( 1 - \frac{1}{Pr_t} \right) \right] \frac{\partial}{\partial y} \left( \frac{u^2}{2} \right)$$

$$H(0) = c_p T_w, \quad H(\infty) = H_e, \quad \left. \frac{\partial H}{\partial y} \right|_{y=\infty} = 0$$

# 3. Physical and Mathematical Modeling

## ➤ Airfoil: Mechanical boundary layer



$$\frac{\partial \bar{u}}{\partial x} + \frac{\partial \bar{v}}{\partial y} = 0$$

$$\bar{u} \frac{\partial \bar{u}}{\partial x} + \bar{v} \frac{\partial \bar{u}}{\partial y} = u_e \frac{du_e}{dx} + \frac{\partial}{\partial y} \left[ (\nu + \nu_t) \frac{\partial \bar{u}}{\partial y} \right]$$

$$\frac{\partial \bar{p}}{\partial y} \approx 0$$

$$\nu_t = l^2 \frac{\partial \bar{u}}{\partial y}$$

$$l = \kappa(y + \Delta y) \left[ 1 - \exp\left(-\frac{y + \Delta y}{A}\right) \right]$$

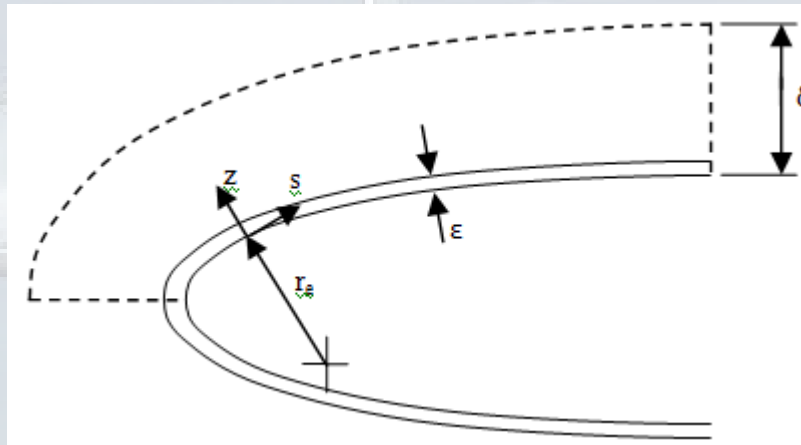
$$\Delta y = 0.9 \frac{\nu}{u_\tau} \left[ \sqrt{k_s^+} - k_s^+ \exp\left(-\frac{k_s^+}{6}\right) \right]$$

$$A = 26 \frac{\nu}{u_\tau N}$$

$$N = \sqrt{1 - 11.8 \frac{\nu u_e}{u_\tau^3} \frac{du_e}{dx}}$$

# 3. Physical and Mathematical Modeling

## ➤ Airfoil: Conjugated Heat Transfer Problem



$$w(z) \frac{\partial T}{\partial t} + w_f u(s, z) \frac{\partial T}{\partial s} + w_f v(s, z) \frac{\partial T}{\partial z} = k(z) \frac{\partial^2 T}{\partial s^2} + \frac{\partial}{\partial z} \left[ k(z) \frac{\partial T}{\partial z} \right] + w_f \frac{\partial}{\partial z} \left[ \frac{l^2}{Pr_t} \frac{\partial u}{\partial z} \frac{\partial T}{\partial z} \right] + G(s, z, t)$$

$$T(s, z, 0) = T_\infty$$

$$\left. \frac{\partial T}{\partial s} \right|_{s=0} = 0; \left. \frac{\partial T}{\partial s} \right|_{s=L} = 0$$

$$-k_s \left. \frac{\partial T}{\partial z} \right|_{z=0} = q_w; T(s, \delta, t) = T_\infty$$

# 4. Solution Methodology

## ➤ Pitot Tube

- Solid – GITT
- Fluid – Karman-Pohlhausen Integral Method
- Needs an iterative process to match the temperatures and heat fluxes at the interface

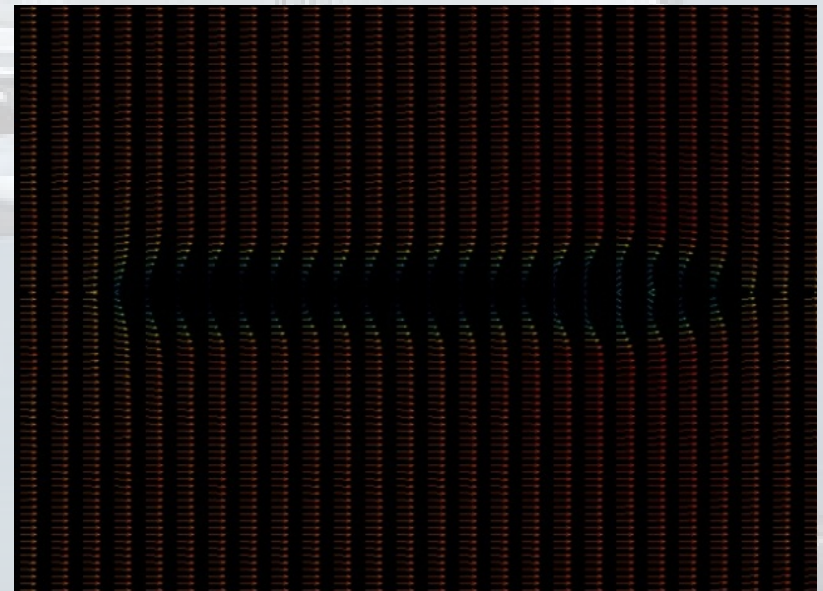
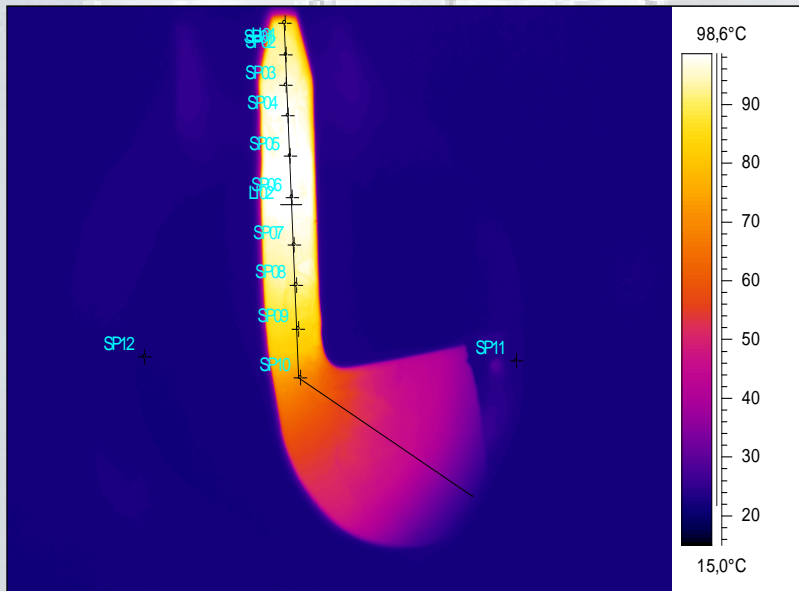
## ➤ Airfoil

- Single Domain Formulation – GITT
- Straightforward and without needing iterative processes



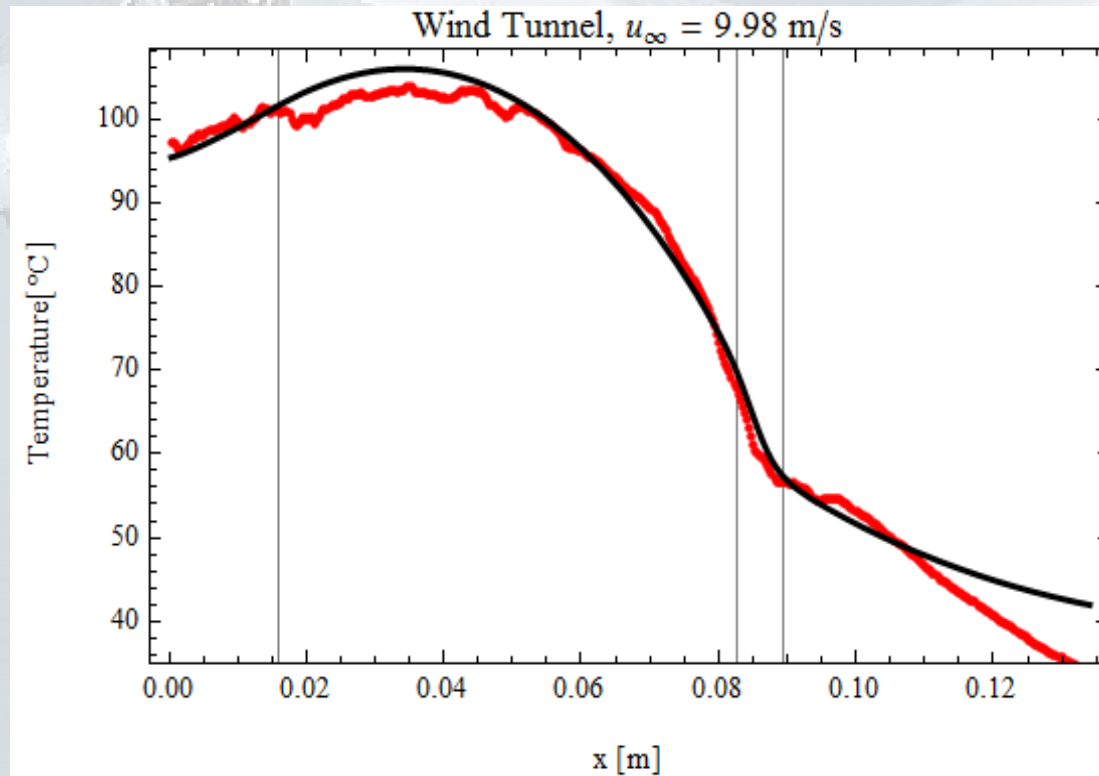
# 5. Results and Discussion

## ➤ Wind Tunnel



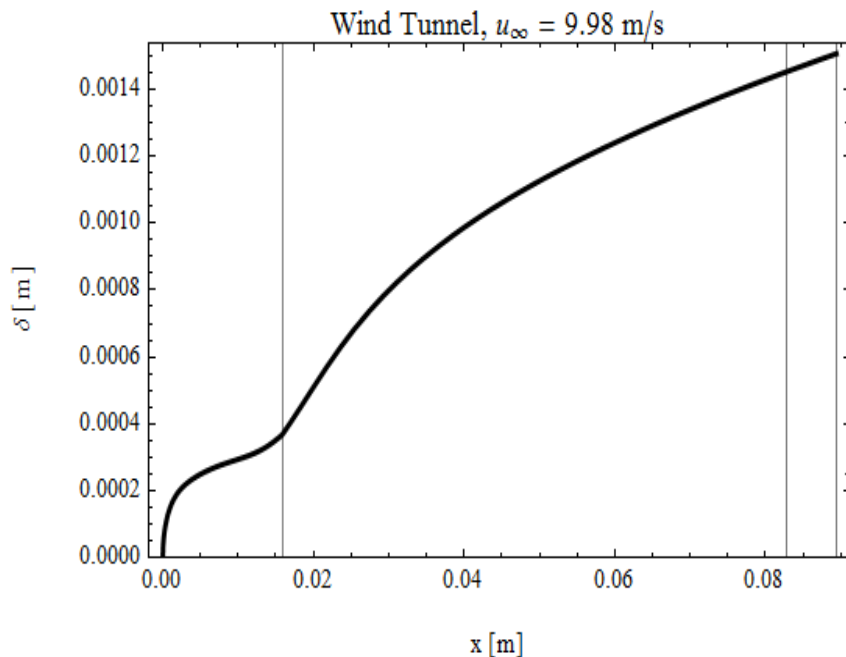
# 5. Results and Discussion

## ➤ Wind Tunnel – INMETRO (10 m/s)

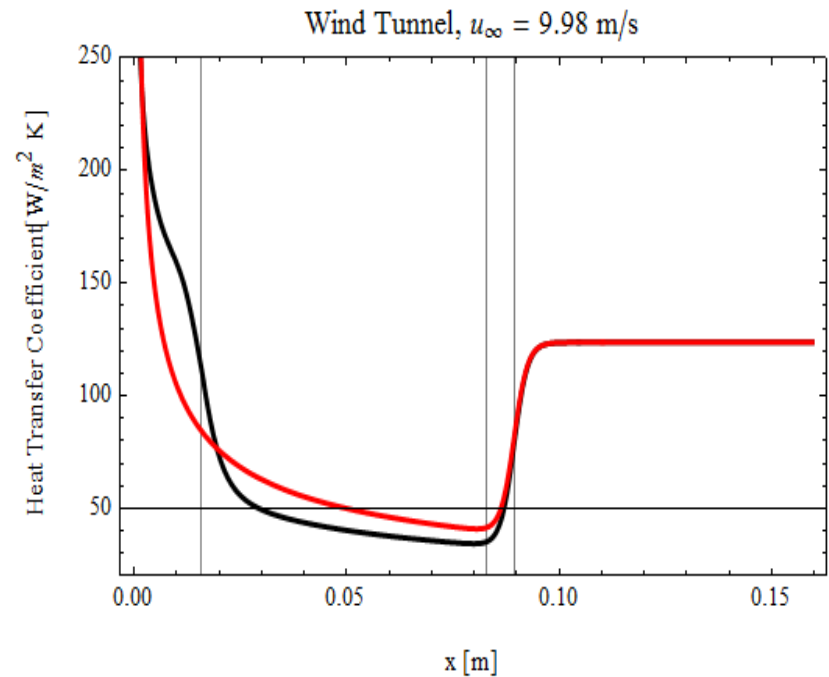


# 5. Results and Discussion

## ➤ Wind Tunnel – INMETRO (10 m/s)



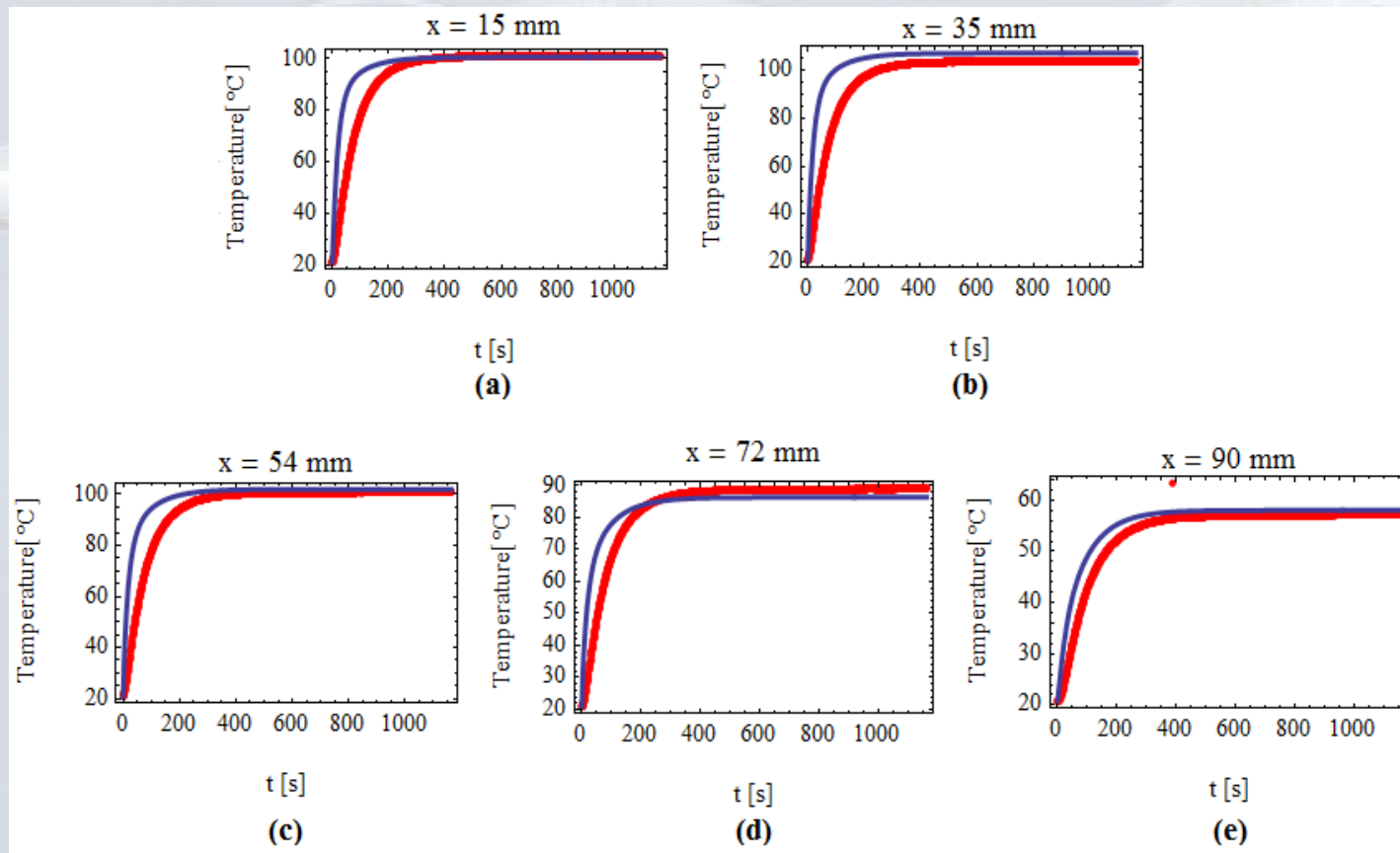
(a)



(b)

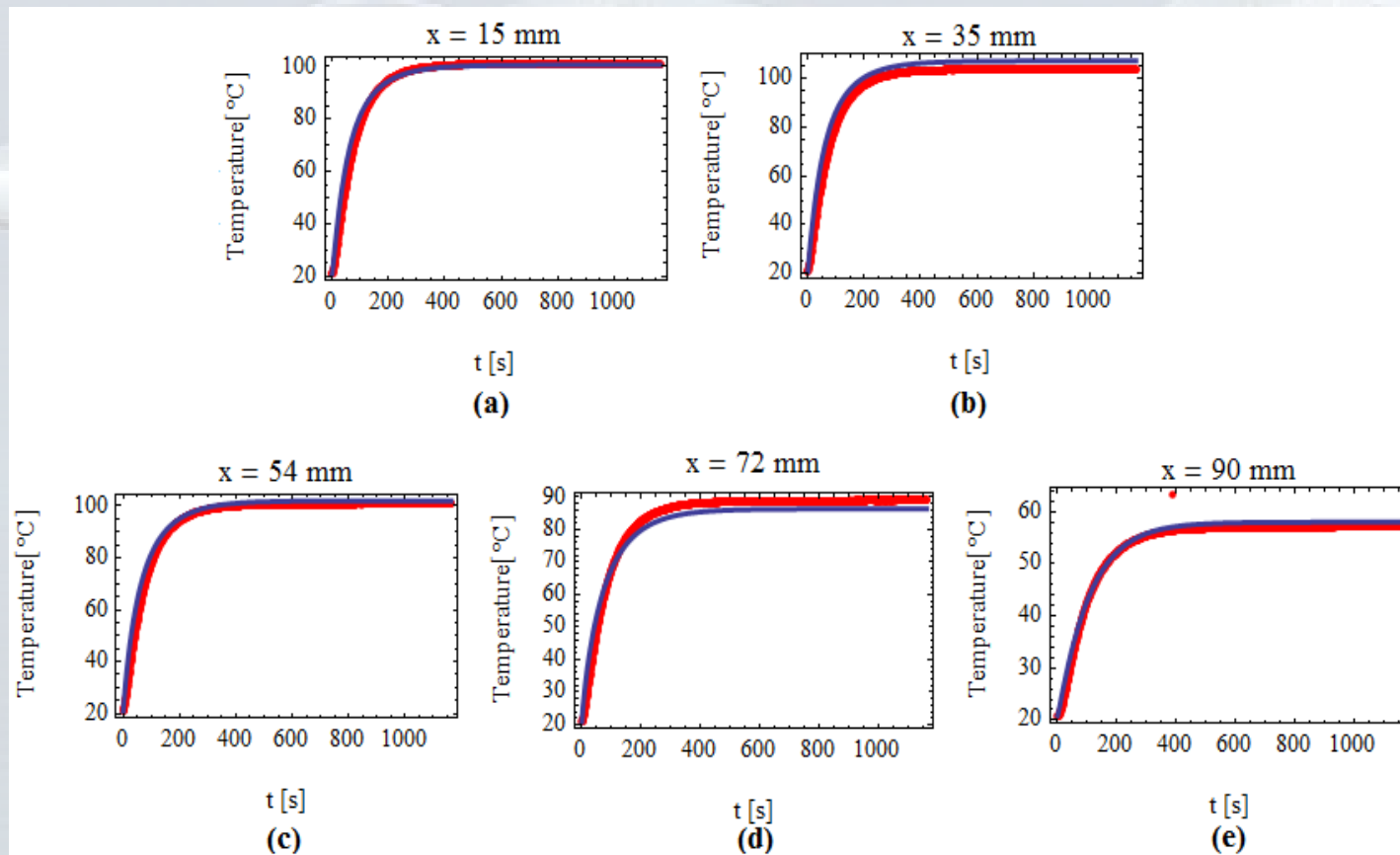
# 5. Results and Discussion

## ➤ Wind Tunnel – INMETRO (10 m/s)



# 5. Results and Discussion

## ➤ Wind Tunnel – INMETRO (10 m/s)



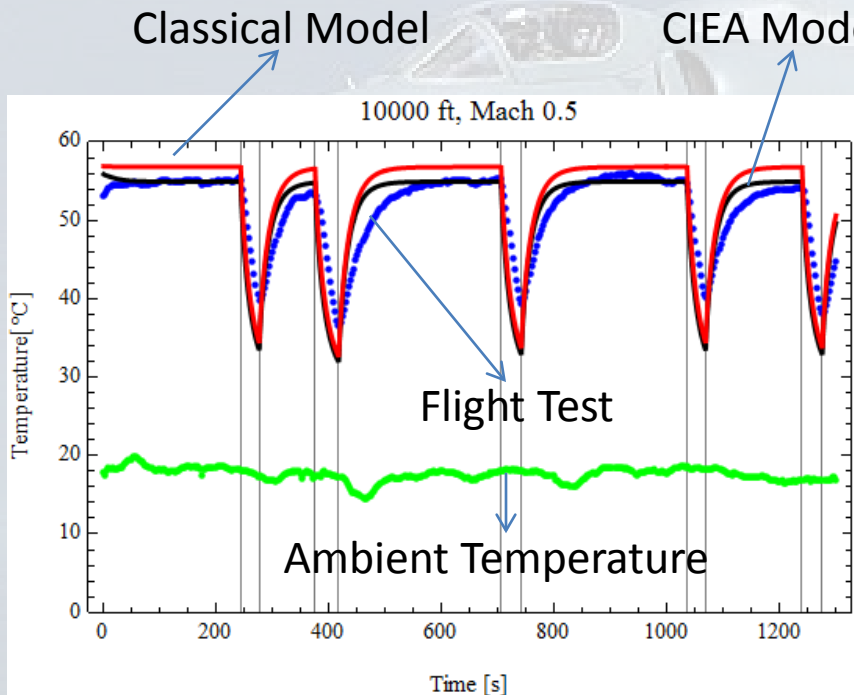
## 5. Results and Discussion

### ➤ A-4 Skyhawk flight tests (Brazilian Navy)

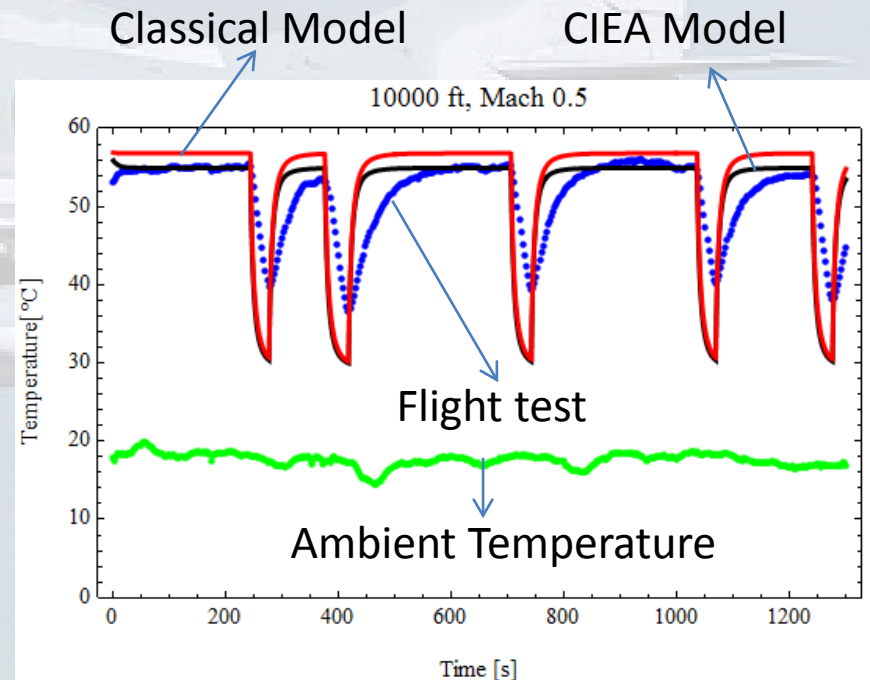


# 5. Results and Discussion

## ➤ A-4 Skyhawk: Mach 0.5, Altitude 10000 ft



**With Porcelain**

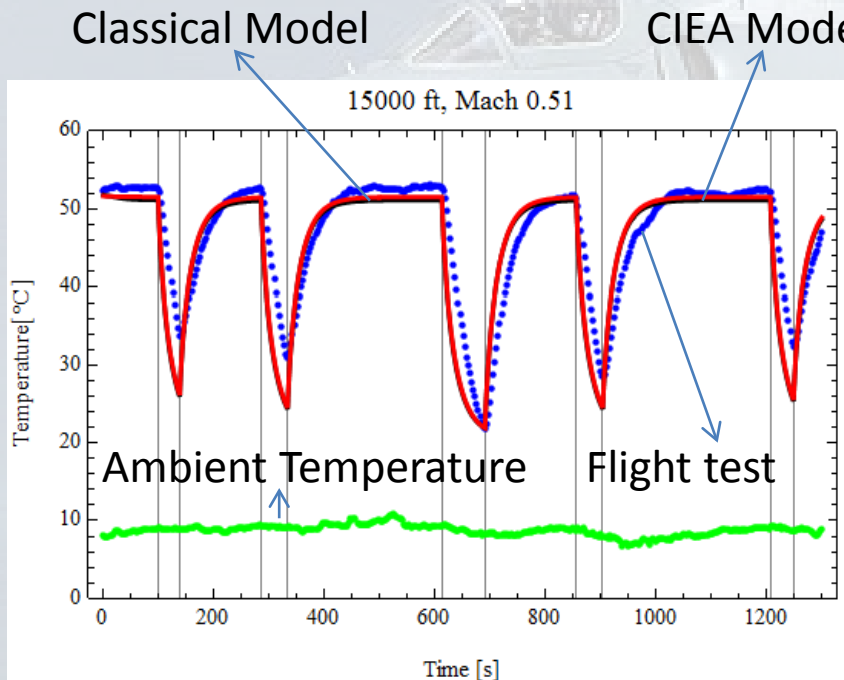


**Without Porcelain**

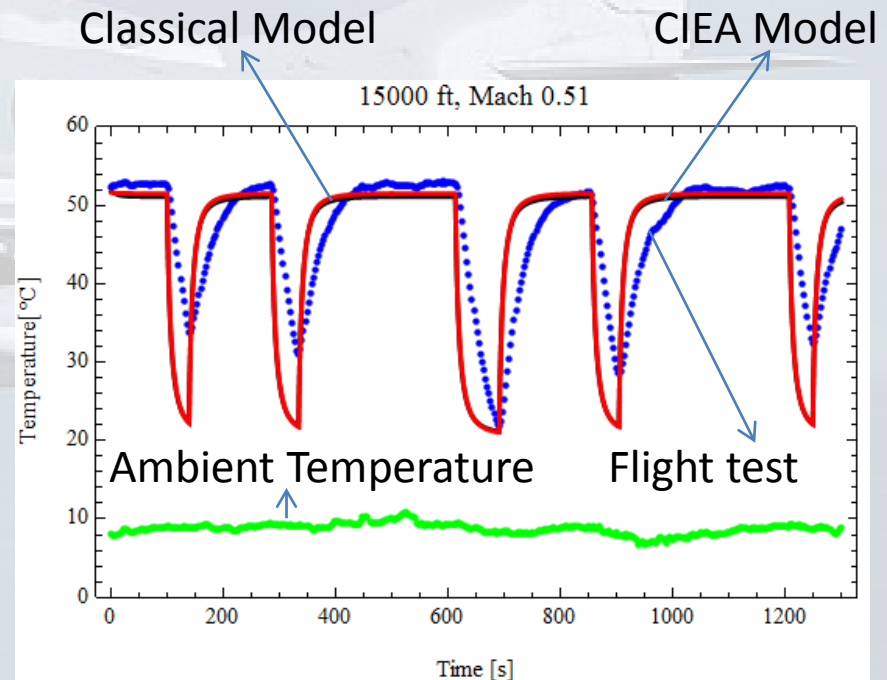


# 5. Results and Discussion

## ➤ A-4 Skyhawk: Mach 0.51, Altitude 15000 ft



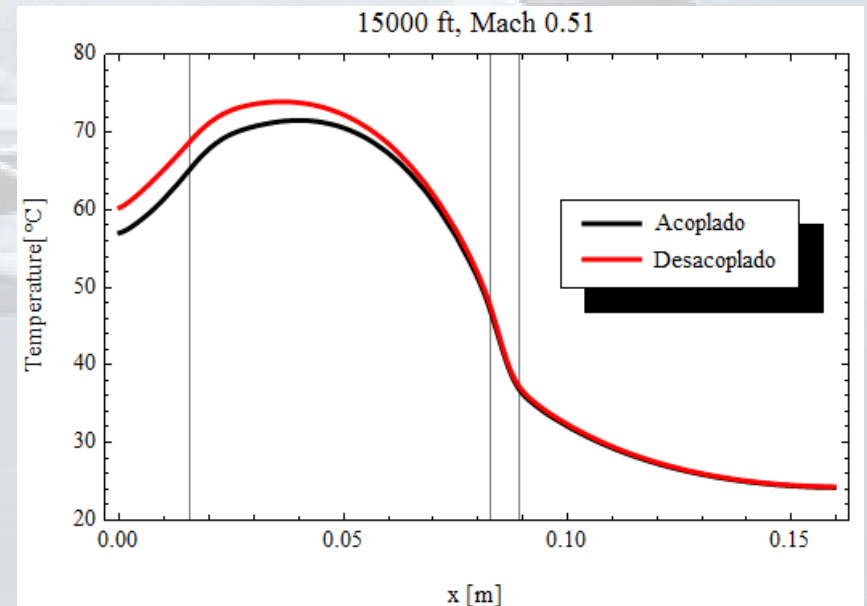
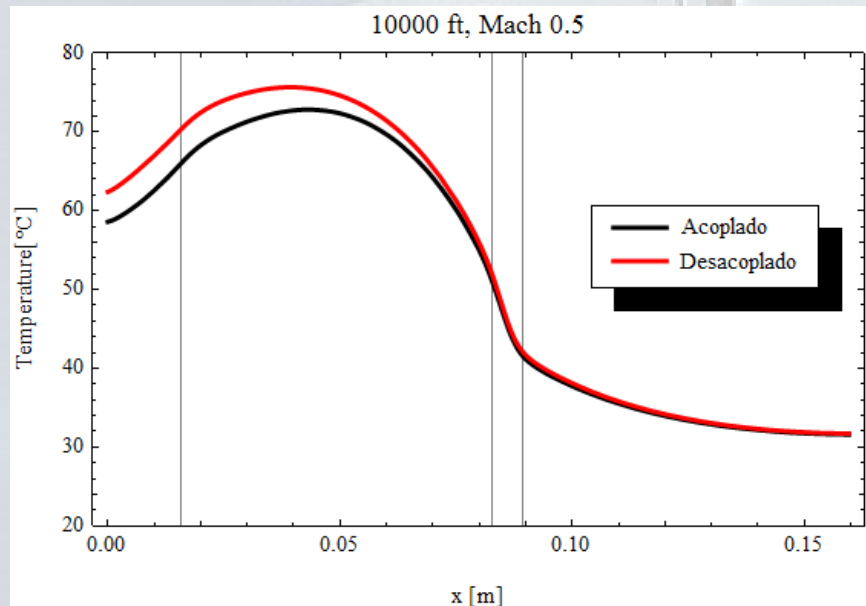
**With Porcelain**



**Without Porcelain**

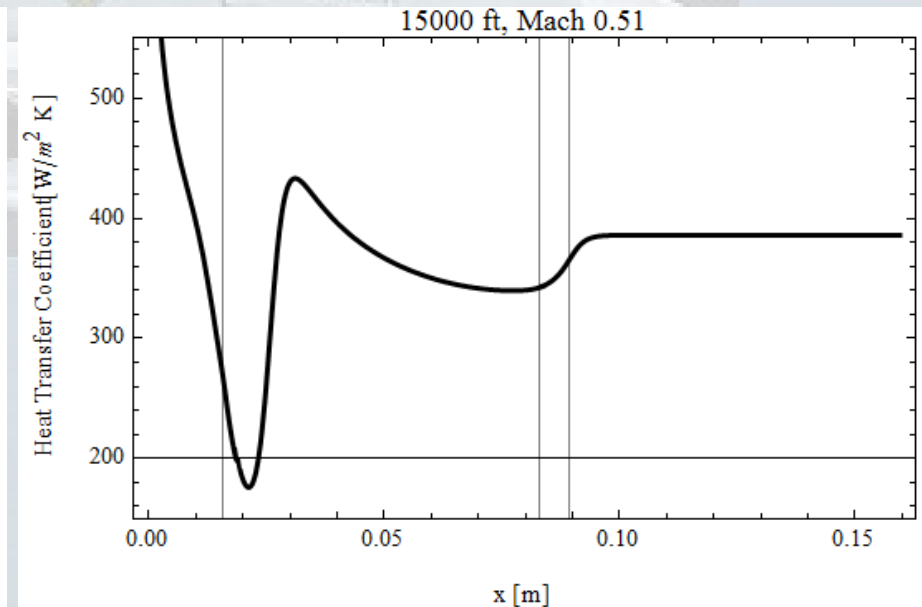
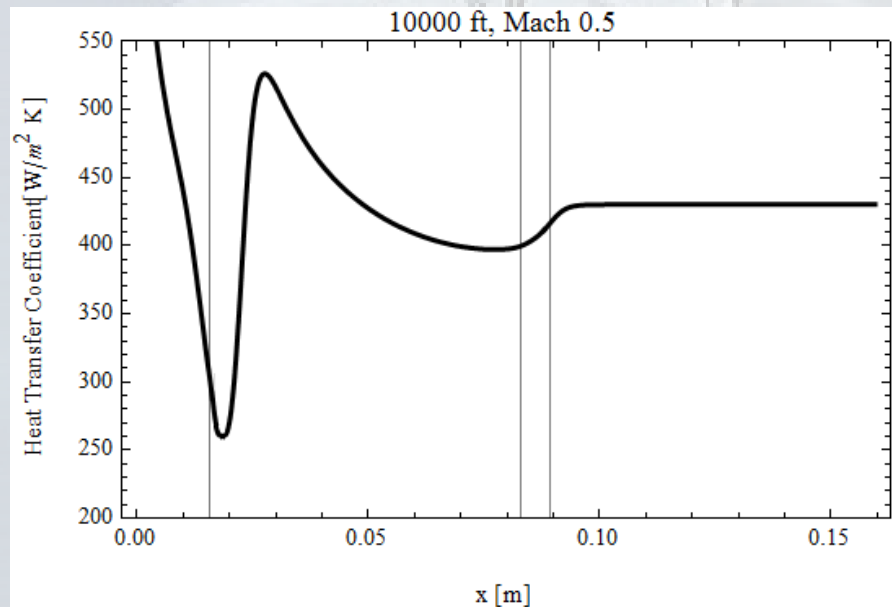
# 5. Results and Discussion

## ➤ A-4 Skyhawk: Steady-state response



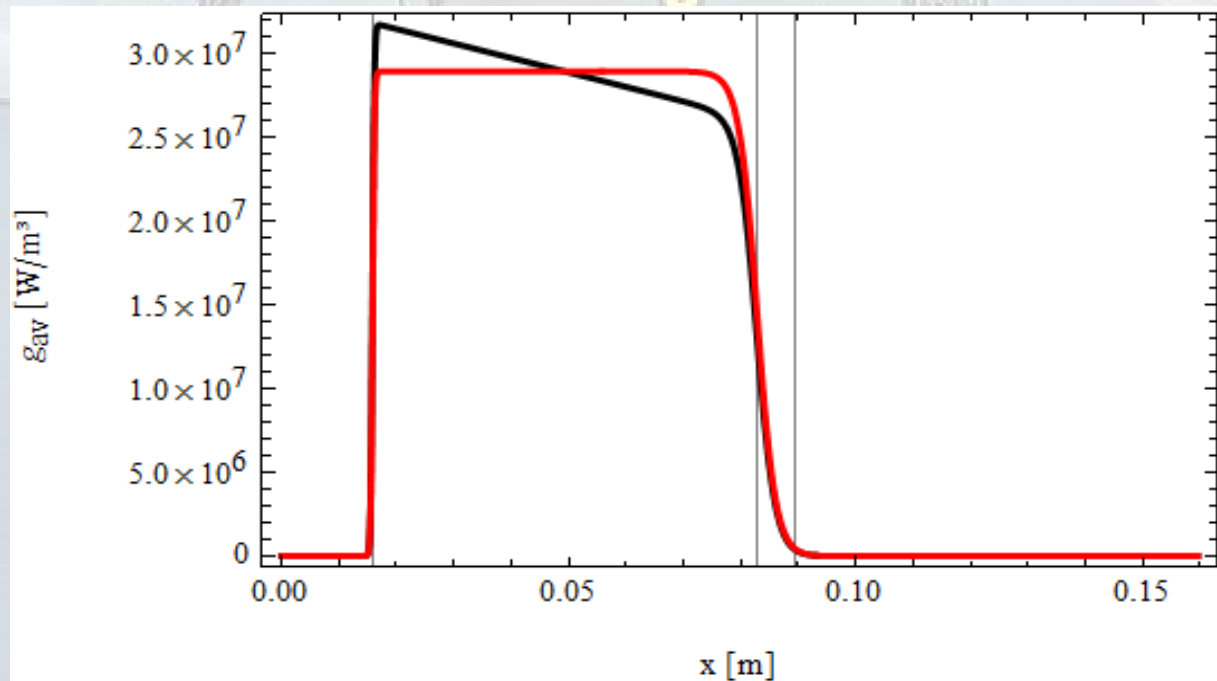
# 5. Results and Discussion

## ➤ A-4 Skyhawk: Heat Transfer Coefficient Distribution



# 5. Results and Discussion

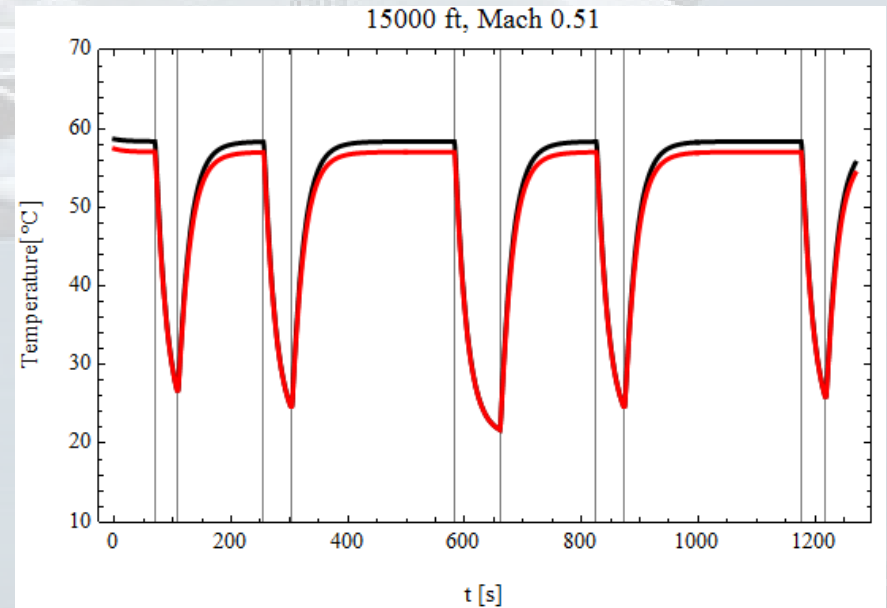
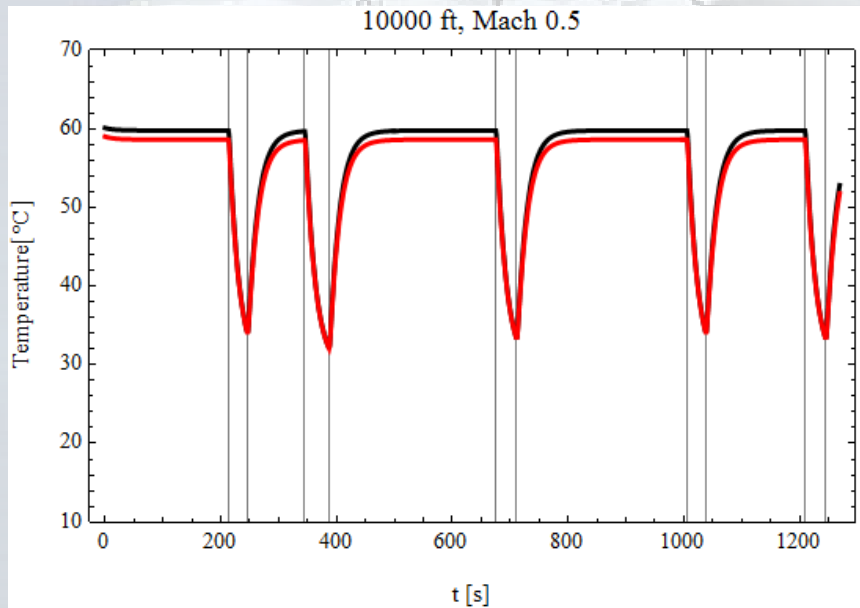
- Parametric Design Studies
  - Power Density



## 5. Results and Discussion

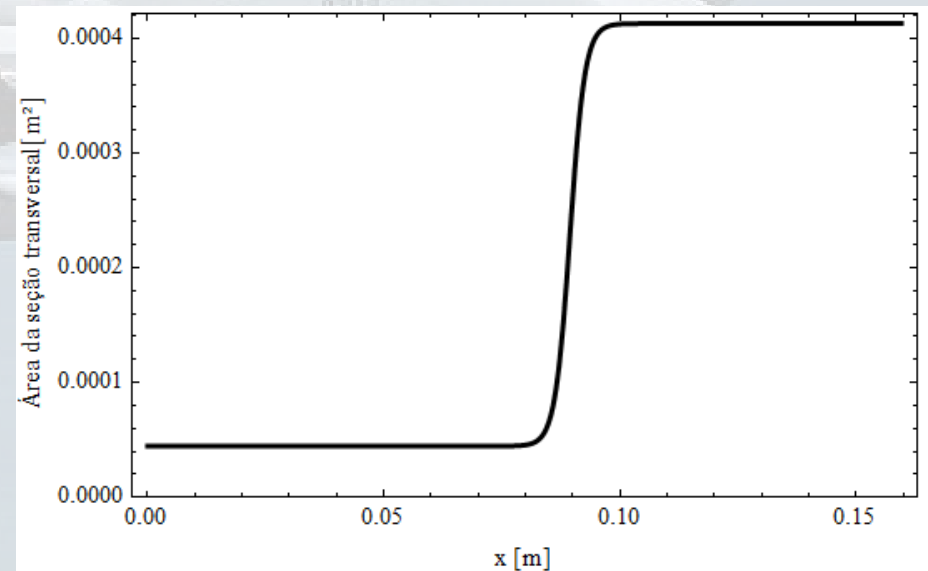
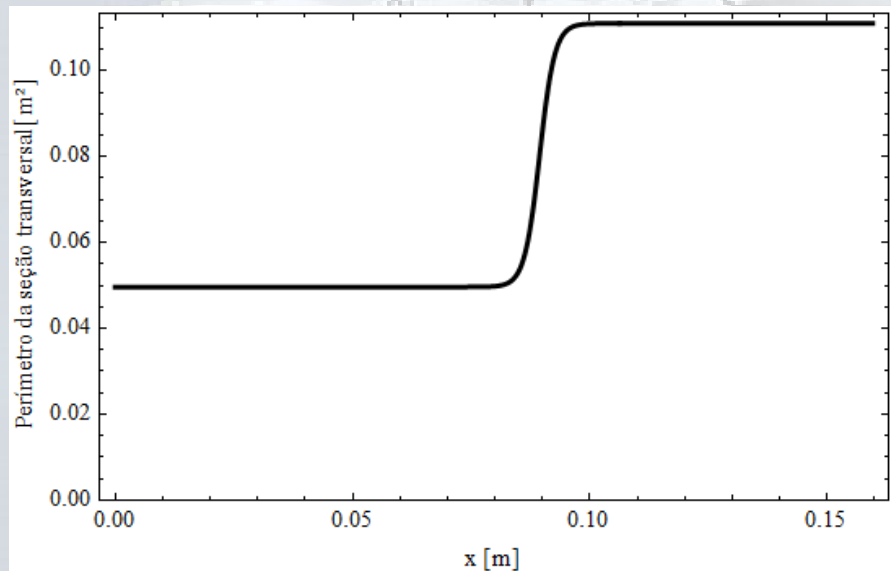
## ➤ Parametric Design Studies

➤ Power Density (Temperature increases 2.3%)



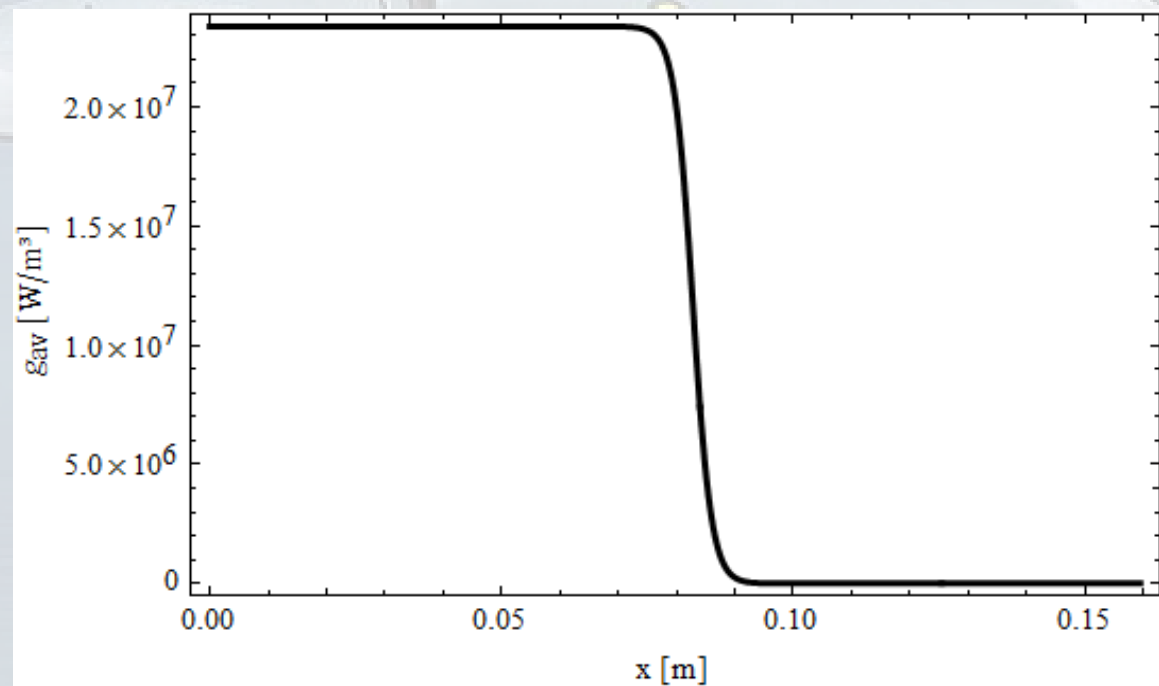
# 5. Results and Discussion

- Parametric Design Studies
  - Fully Cylindrical Probe



# 5. Results and Discussion

- Parametric Design Studies
  - Fully Cylindrical Probe

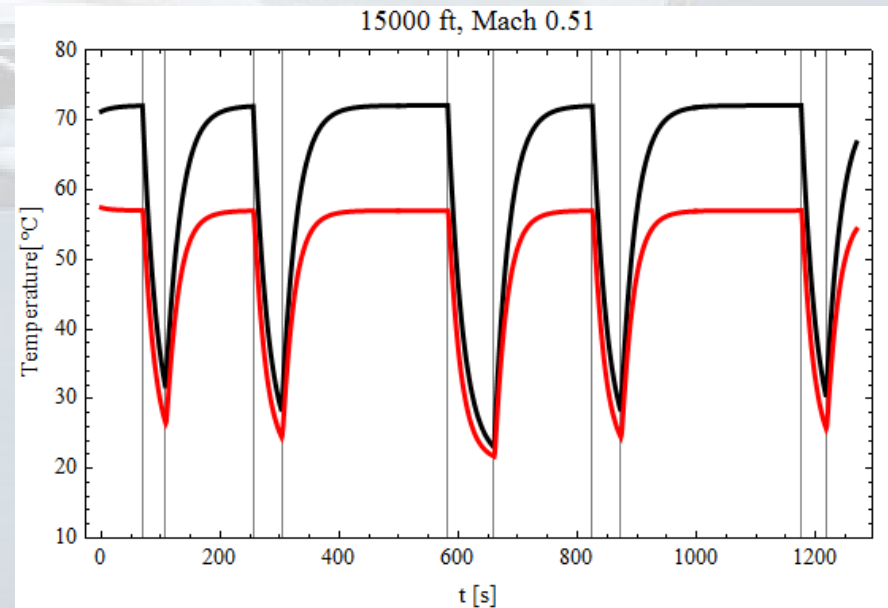
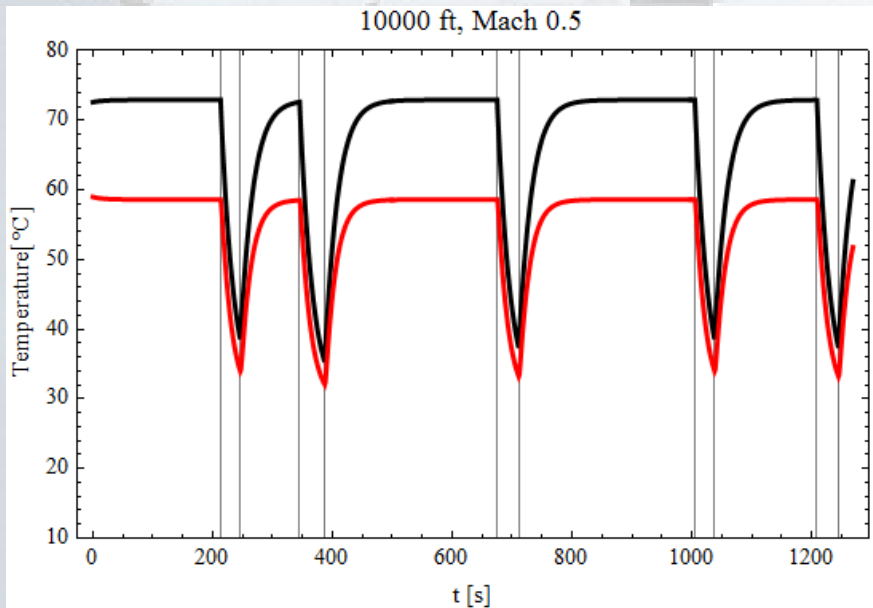




# 5. Results and Discussion

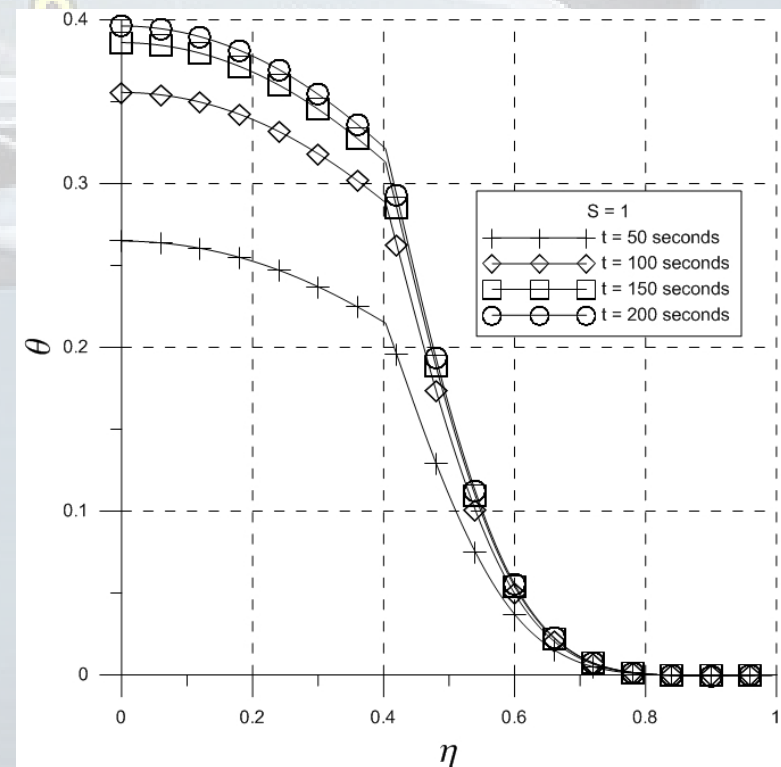
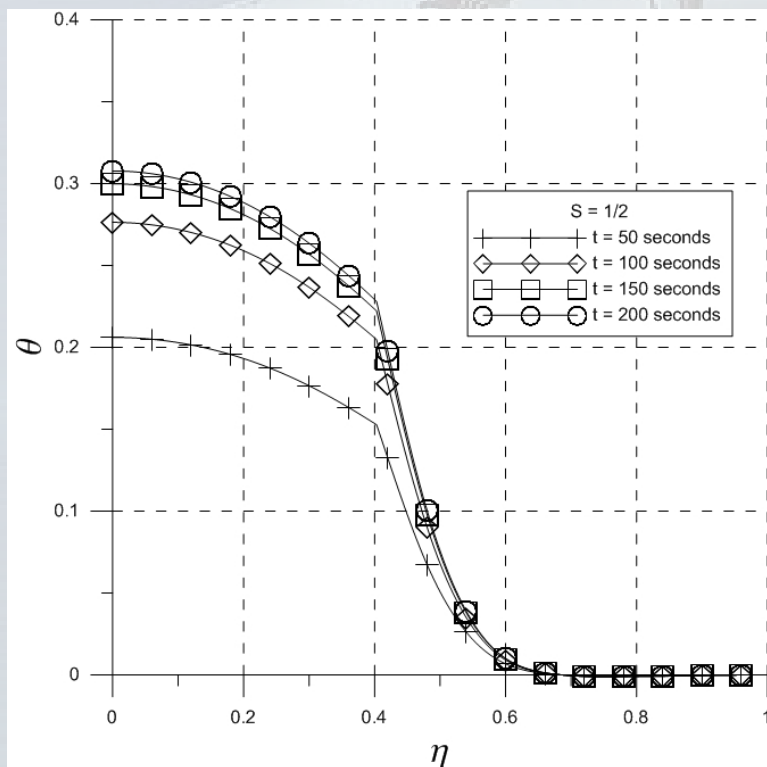
## ➤ Parametric Design Studies

### ➤ Fully Cylindrical Probe (Temperature Increases 26%!!!)



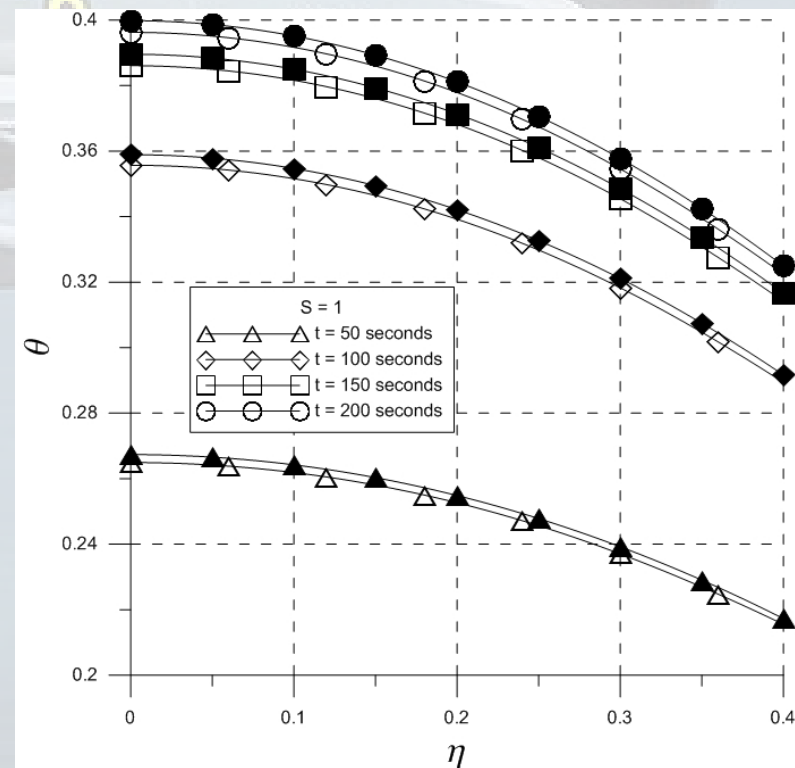
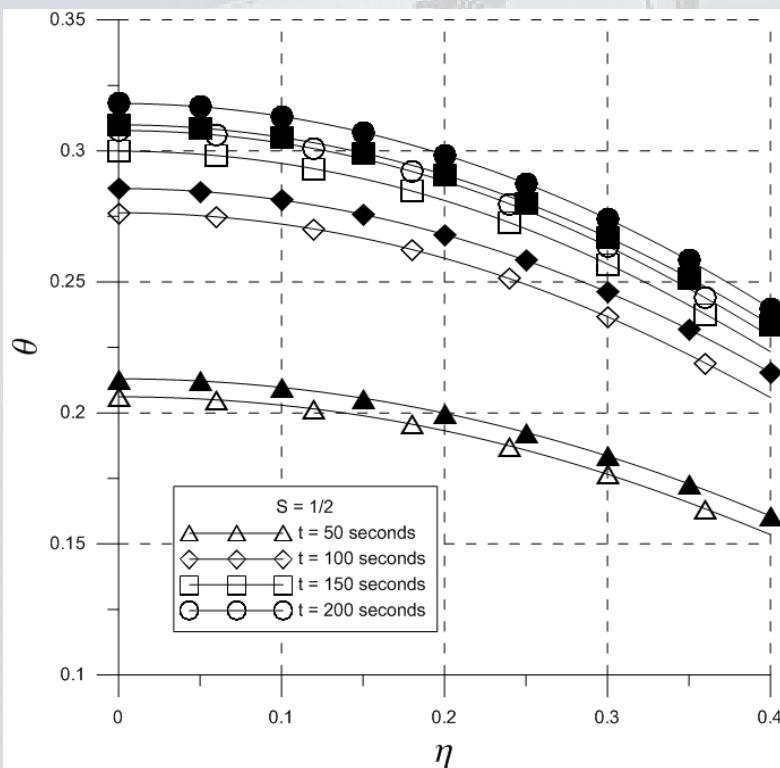
# 5. Results and Discussion

- Single Domain – Airfoil
- Laminar Boundary Layer



# 5. Results and Discussion

- Single Domain – Airfoil
- Laminar Boundary Layer



## 6. Conclusions

- A physical and mathematical model to reproduce the thermal behavior of aircraft surfaces was built and validated
- An important conclusion about the importance of taking into account the solid wall participation on the development of the fluid flow was made based on the conjugated heat transfer model proposed
- The analysis performed allowed the discovery of important directions to be considered in the design of Pitot tubes for icing environment reliability

A faint, grayscale background image of a submarine on the surface of the ocean. The submarine is viewed from a side-on perspective, showing its hull, conning tower, and various antennas. The water is calm, and the horizon is visible in the distance.

Thanks for the attention!!