

# Ice Accretion and Wing Anti-Icing System Simulation

First Workshop on Aviation Safety (WAS),  
June 1st and 2nd, Rio de Janeiro, RJ, Brazil  
Organization COPPE/UFRJ

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- Motivation

Conception, development and certification of anti-icing and de-icing wing systems.

Modeling and simulation of anti-icing and de-icing systems.

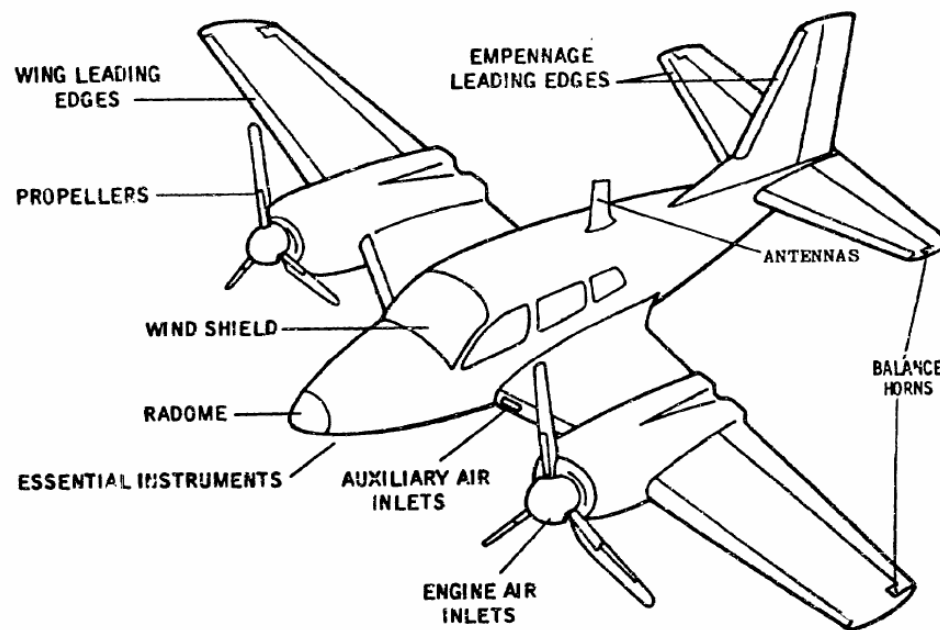
Modeling and simulation of ice accretion in airplane wings and components.

Heat and mass transfer and liquid water runback.

Brazilian aeronautic industry



## Aircraft Ice Accretion

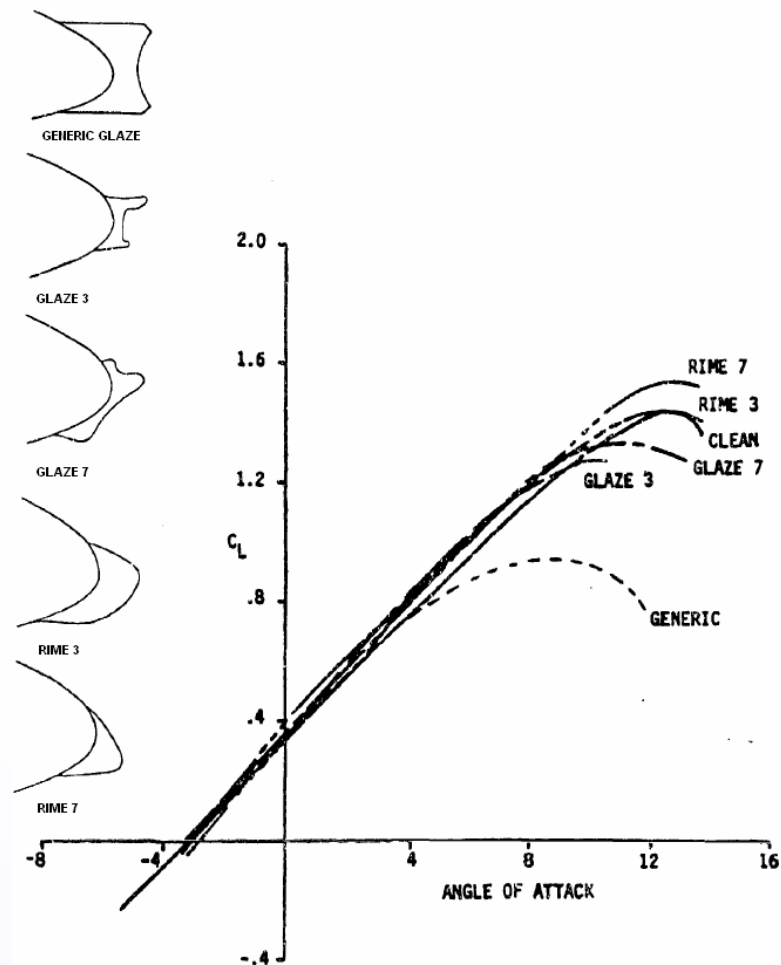


- Condition for icing accretion
  - Subcooled water droplets
  - Non-protected Surfaces
  - Failure of Anti-icing system
- Consequences
  - Aerodynamic degradation
  - Weight increase
  - Ice shedding
  - Sensors malfunction

Source: Aircraft Icing Handbook Vol2  
DOT/FAA/CT-88/8-2



## Ice Accretion Effects



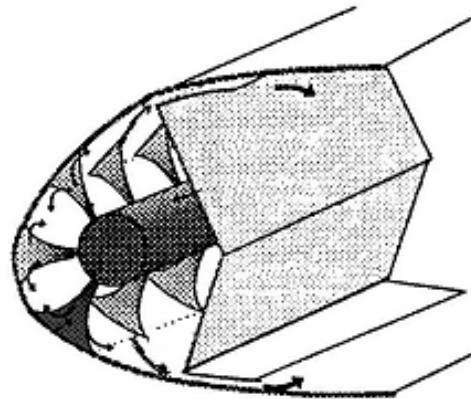
Source: Aircraft Icing Handbook Vol1,  
DOT/FAA/CT-88/8-1



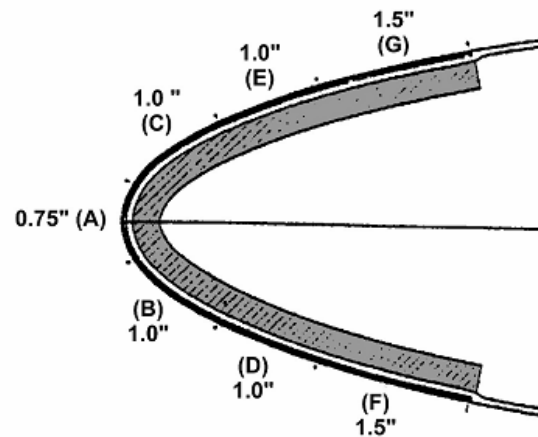
# Anti-icing and De-icing Systems

## Thermal Ant-icing and De-icing Systems

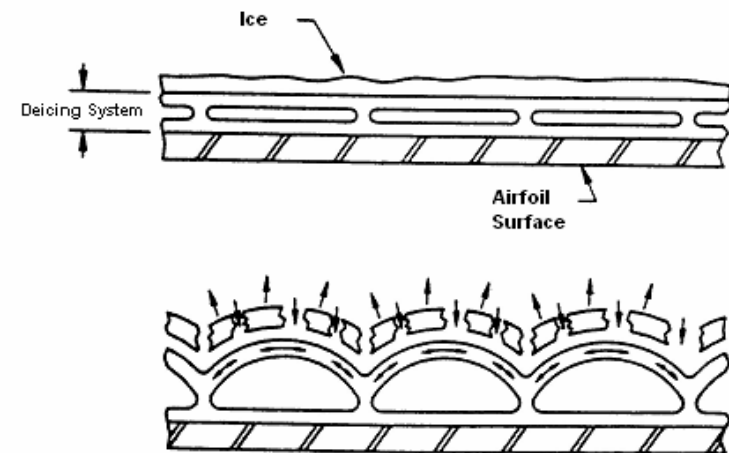
### Piccolo Tube



### Electrical Resistance

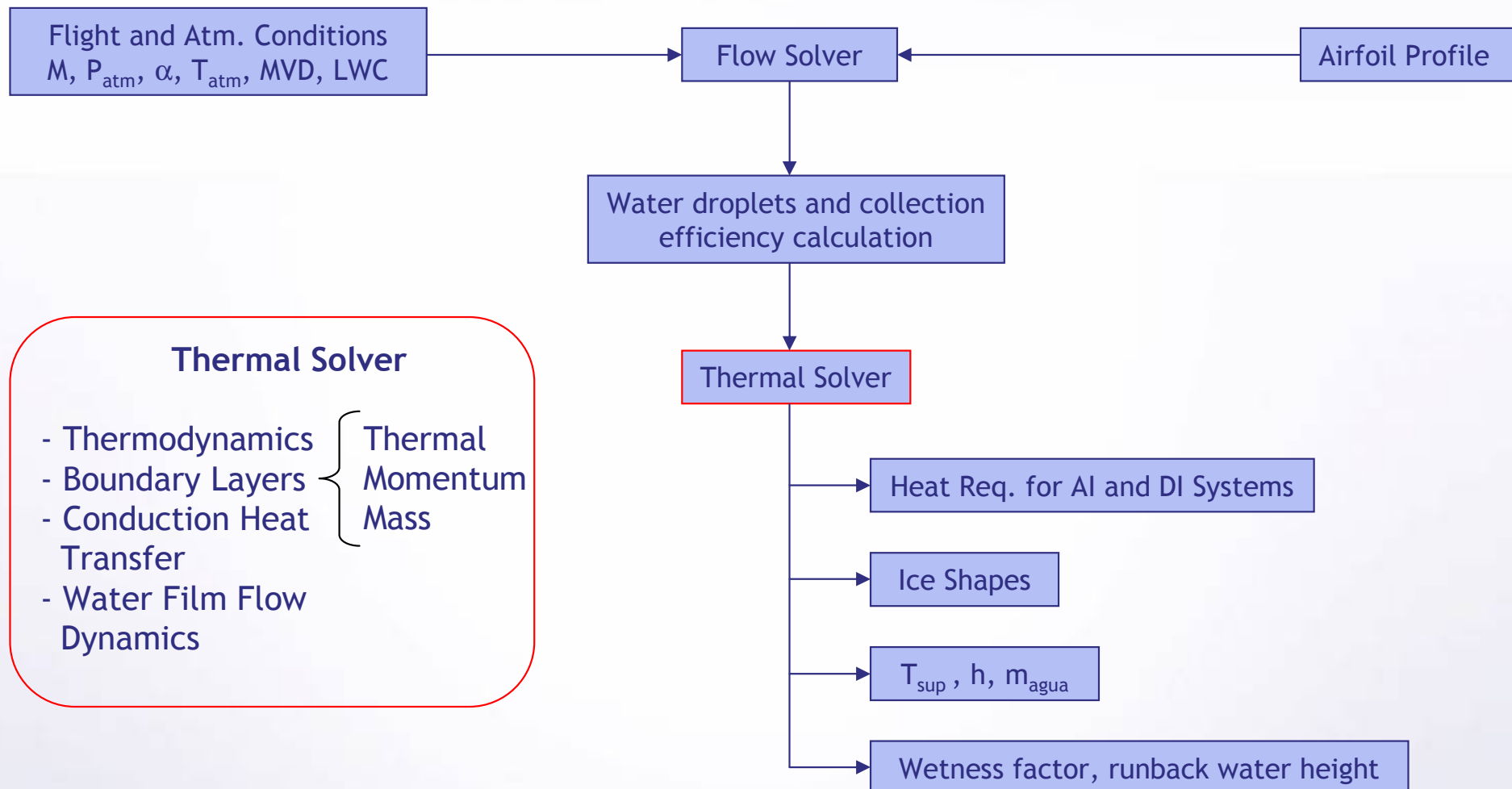


## Mechanical De-icing System



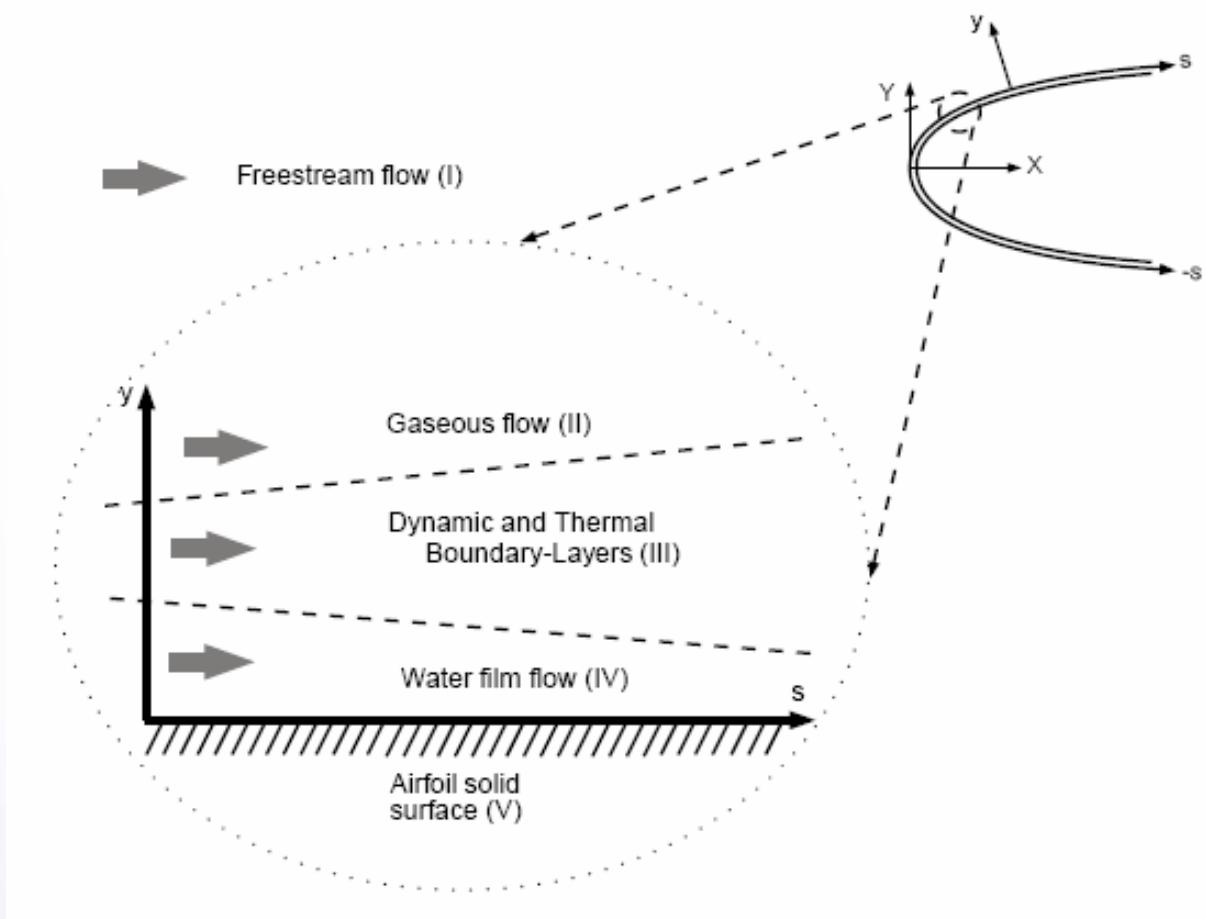


# Anti-icing and icing accretion Simulation





## Modeling Domains







## Icing and Anti-Icing Codes

Code	Authors	Characteristics			
		Boundary Layer	Wetness Factor	Lam-Turb Transition	Onset / Length
ANTICE	Al-Khalil et al. (2001)	not calculated (exp. data)	rivulets	not calculated	not calculated
ONERA	Henry (1992)	diferential	not calculated	no info	no info
CANICE FD	Morency, Tezok e Paraschivoiu (1999)	diferential (Cebeci, 1971)	not calculated	intermittency (Chen,Thyson,1971)	w/o freestream turbulence effect (Michel.1951)
M.Sc.Silva (1998-2002)	Silva (2002)	integral (Ambrok,1957)	not calculated	Probabilistic (Reynolds, Kays, Kline,1958b)	adjusted
Ph.D.Silva (2003-2009)	Silva (2009)	integral (Ambrok,1957), superposition (Reynolds, Kays, Kline,1958) and diferential (Cebeci, Cousteix, 2005)	rivulets	intermittency (Reynolds, Kays, Kline, 1958) and (Abu-Ghannam, Shaw, 1980)	adjusted and predicted (Abu-Ghannam, Shaw,1980)
LEWICE	Macarthur, Keller, Luers (1982)	integral (Makkonen)	not calculated	abrupt	$Re_{ks}$
ONERA	Guffond, Brunet (1988)	integral (Makkonen)	not calculated	abrupt	$Re_{ks}$
M.Sc. Stefanini (2006-2009)	Stefanini (2009)	integral (Makkonen)	not calculated	abrupt, intermittency (Abu-Ghannam, Shaw, 1980)	$Re_{ks}$ , adjusted

# Thermal Solver Development

- Thermal Boundary Layer
  - Non-isothermal surface
  - Effect of pressure gradient
  - Effect of mass transfer
  - Effect of surface roughness
  - Effect of the laminar-turbulent transition
  - Effect of the compressibility
- Water Runback Flow
  - Water film flow and breakdown
  - Rivulets flow



## Laminar-Turbulent Transition

- Algebraic correlations of Abu-Ghannam and Shaw (1980) for intermittency function

$$\gamma(\text{Re}) = 1 - \exp(-5\eta^3)$$

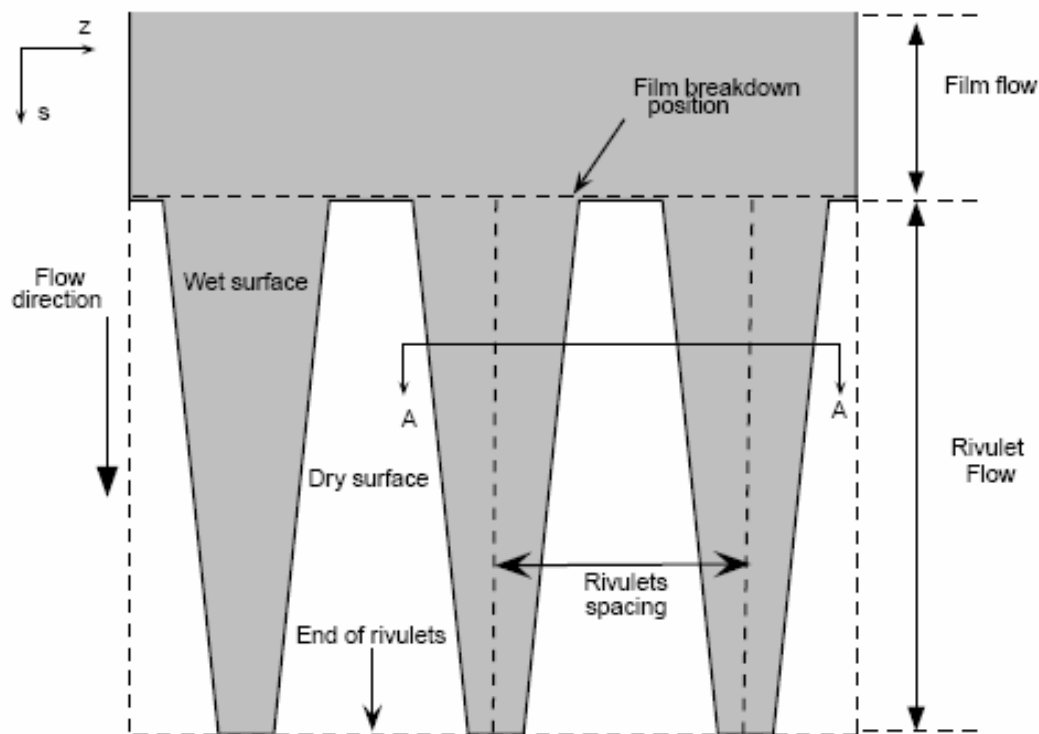
$$\eta = \frac{\text{Re}_s - \text{Re}_{s,tr}}{\text{Re}_{s,t} - \text{Re}_{s,tr}}$$

- In the laminar-turbulent transition region the Stanton number ( $St$ ) is calculated using the intermittency function

$$St(\text{Re}) = [1 - \gamma(\text{Re})] \cdot St_{lam} + \gamma(\text{Re}) \cdot St_{turb}$$



## Film breakdown and Rivulets formation



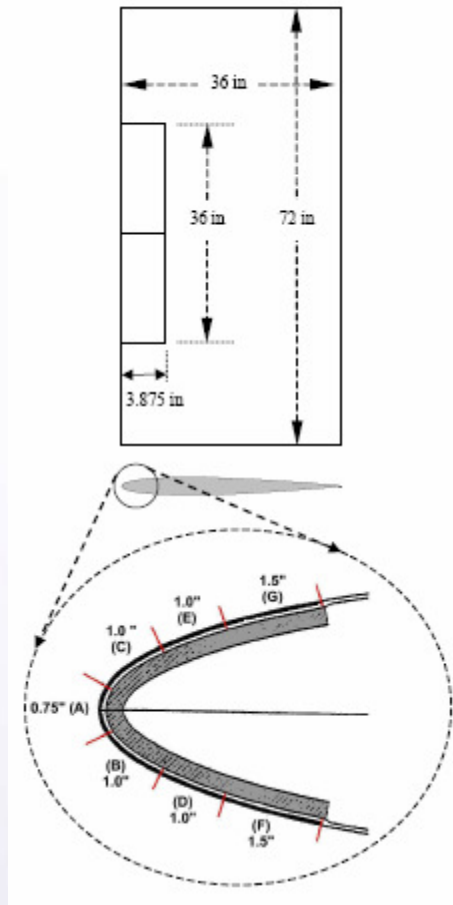
- The film height varies with evaporation, temperature, pressure gradient and shear stress
- The rivulets will form when the film reaches critical height
- The dry and wet areas ratio affect heat transfer
- The water film breakdown occurs only downstream from impingement limits (Al-Khalil, 1991)

$$F = \frac{A_{wet}}{A_{total}}$$

$$A_{total} = A_{wet} + A_{dry}$$



## Anti-icing simulation - Selected test cases

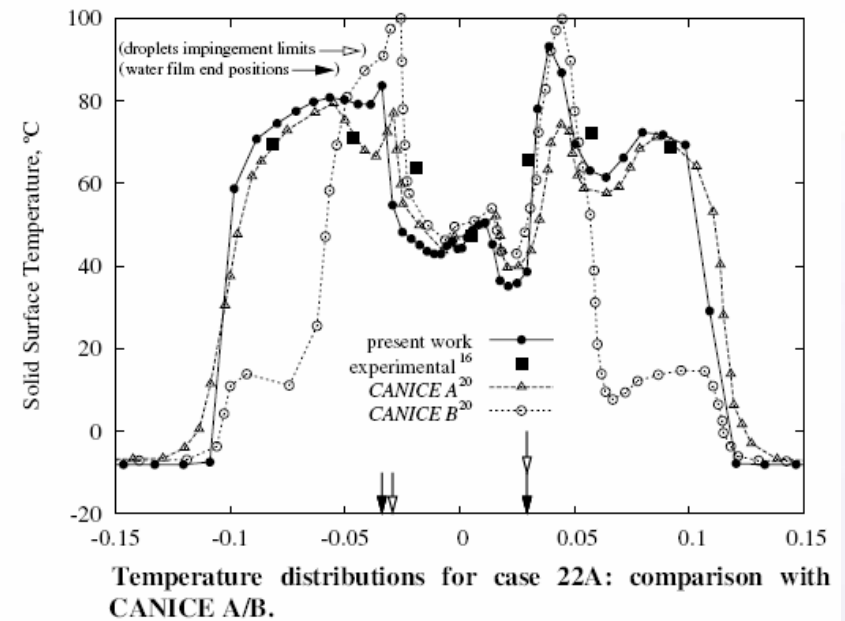
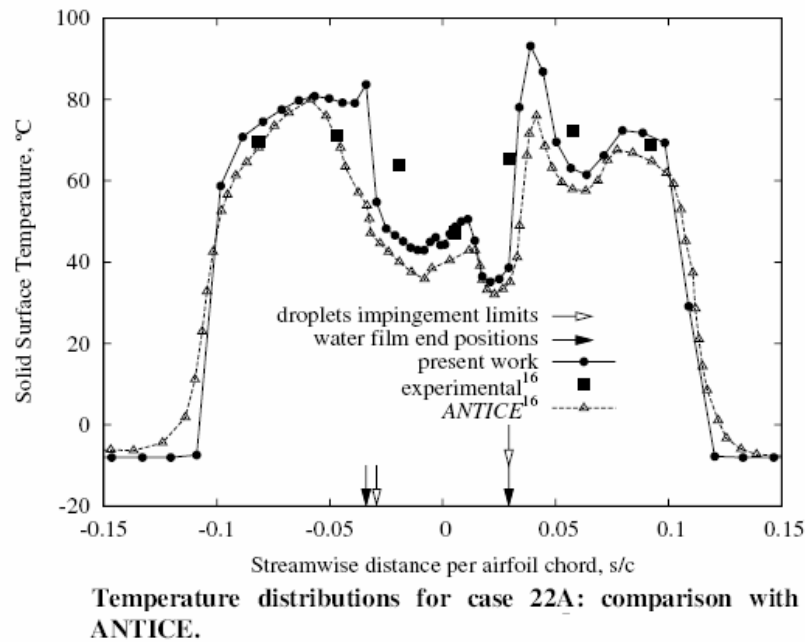


- Tests performed by Al-Khalil et al. (2001)
- NASA IRT Cleveland, OH, USA
- NACA0012 electrically heated
- Test series used to validate Lewice/Antice code

Parameter	22A	67A / 67B
$V_{inf}$ [m/s]	44.7	89.4
$T_{tot}$ [K]	264.4	251.5
$\alpha$	$0.0^\circ$	$0.0^\circ$
LWC [ $g/m^3$ ]	0.78	0.55
MVD [ $\mu m$ ]	20.0	20.0
Turb. Level $Tu$	3.1%	3.1 and 3.0 %
$(s/c)_{prot}$	$\sim 10\%$	$\sim 10\%$
$Re_{c, prot}$	$6.72 \cdot 10^5$	$1.38 \cdot 10^6$
Q elec. aver. [ $kW/m^2$ ]	19.3	25.9 / 11.1
Mach	0.1369	0.2813



## Basic B.L. Integral Model

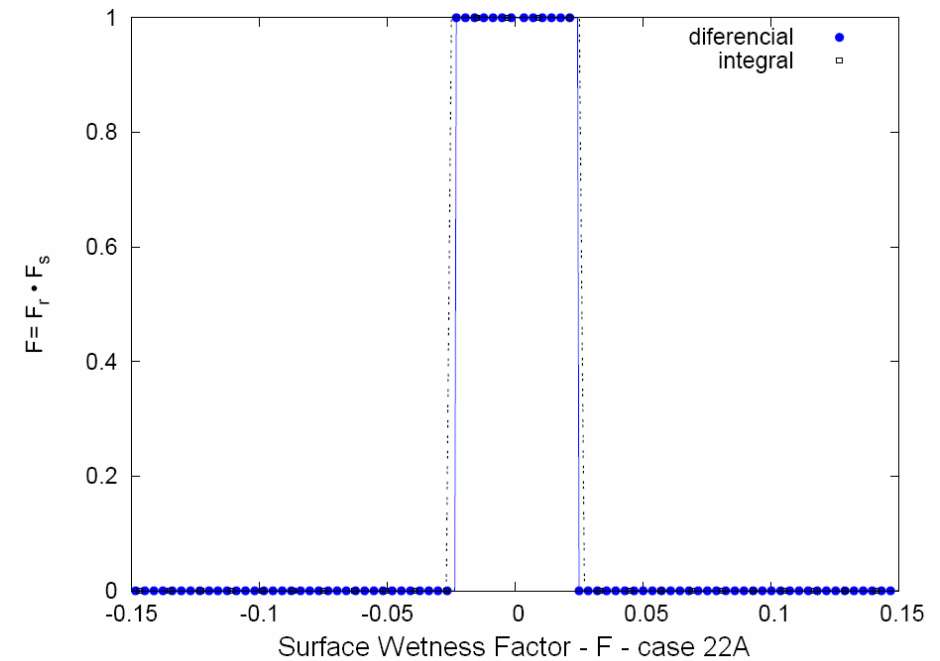
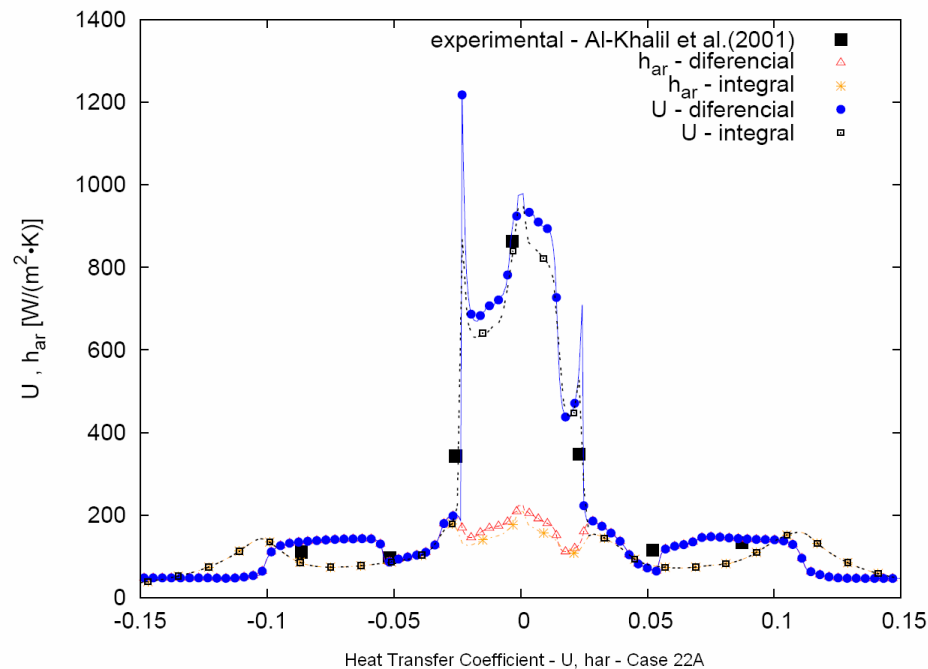


## Comparison with ANTICE and CANICE A/B - case 22A

Note - Basic Model: smooth, w/o rivulet and w/o lam-turb transition prediction



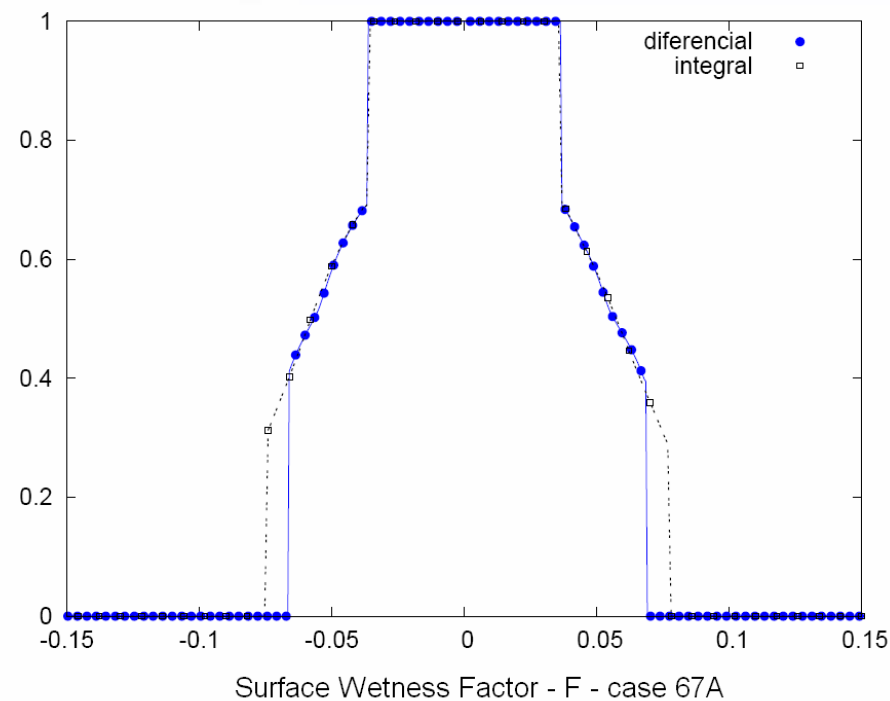
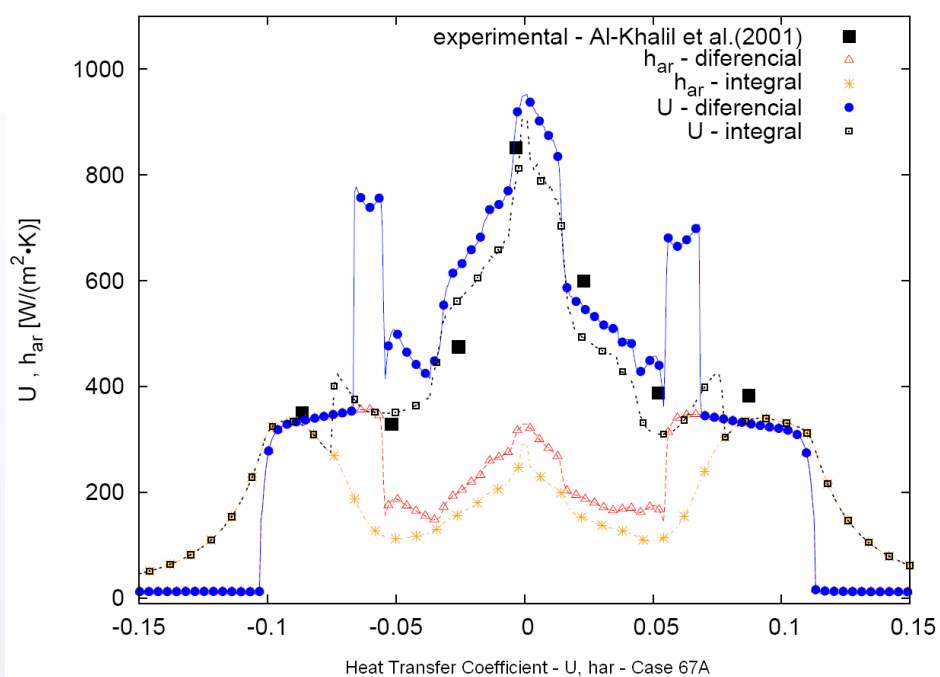
## Diferencial B.L. model with Rivulet model



## Comparison with Antice - case 22A



## Diferencial B.L. model with Rivulet model

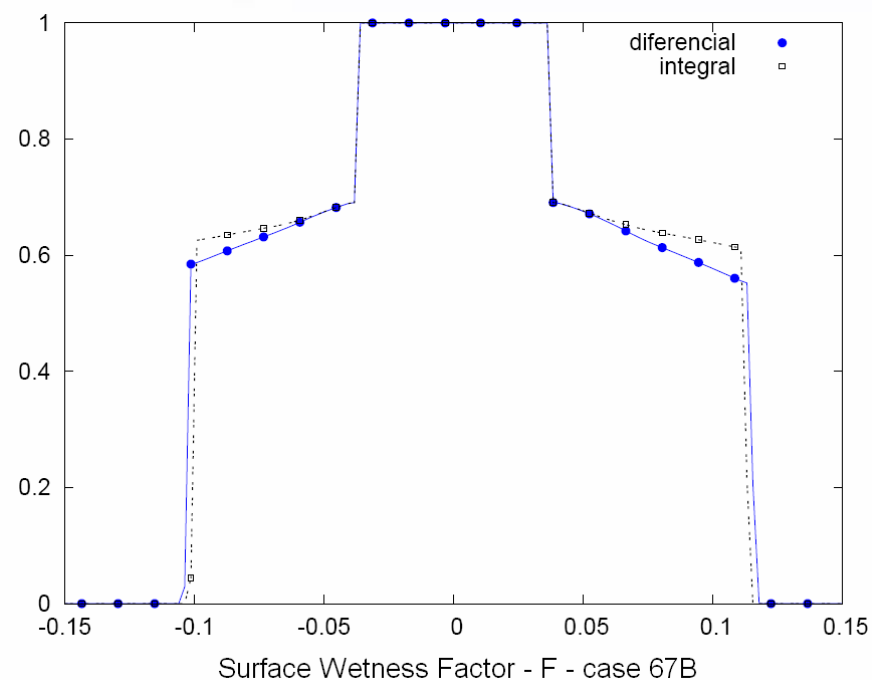
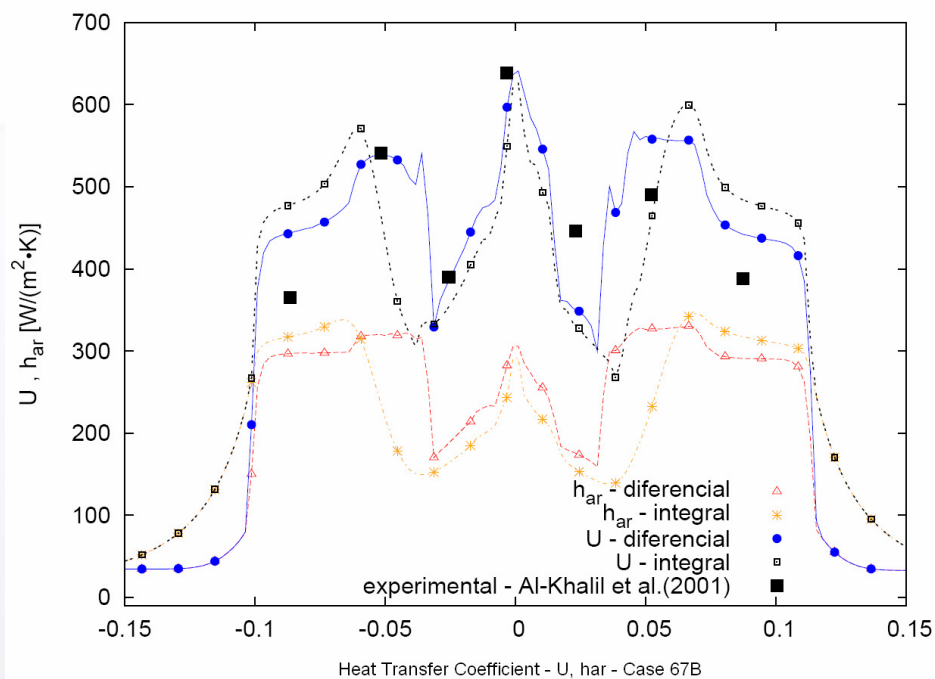


## Comparison with Antice - case 67A





## Diferencial B.L. model with Rivulet model



## Comparison with Antice - case 67B

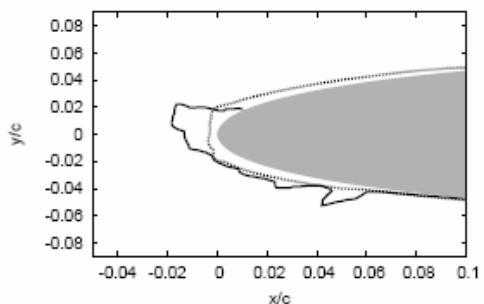
## Icing accretion simulation - Selected test cases

- Kind (2001) published the results of a comprehensive comparison between icing codes and experimental data measured at several test conditions and icing tunnels around the world.
- Shin and Bond (1994) changed the free stream tunnel static temperature and liquid water content to evaluate the IRT-NASA results repeatability.

Parameter	Kind C13	Kind C14	Shin F01
$V_{inf}$ [m/s]	67.0	57	67.1
$T_{inf}$ [K]	264.4	267.6	Variable
$\alpha$	$0.0^\circ$	$0.0^\circ$	$4.0^\circ$
LWC [g/m <sup>3</sup> ]	0.65	1.04	1.00
MVD [ $\mu$ m]	40.0	27.73	20.0
Duration [s]	672.0	247.2	360.0
Airfoil	NACA0012	NACA0012	NACA0012

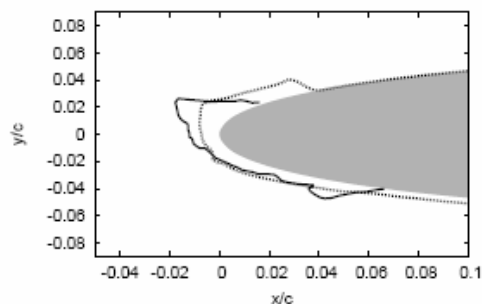


## Basic B.L. model with Abrupt Transition



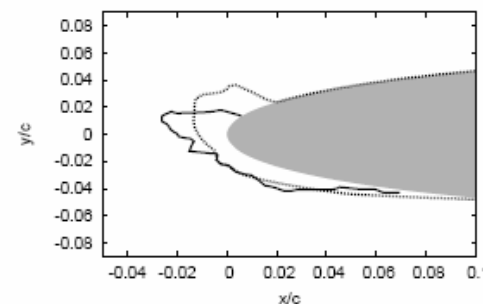
Experimental — Present Work ·····

$$T_{\infty} = 270,9 \text{ K}$$



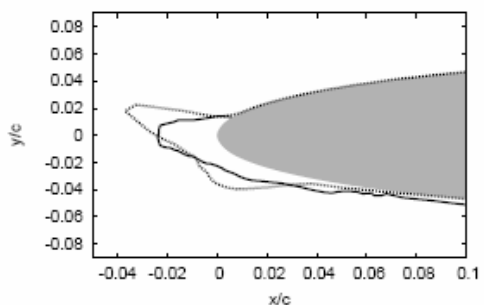
Experimental — Present Work ·····

$$T_{\infty} = 269,3 \text{ K}$$



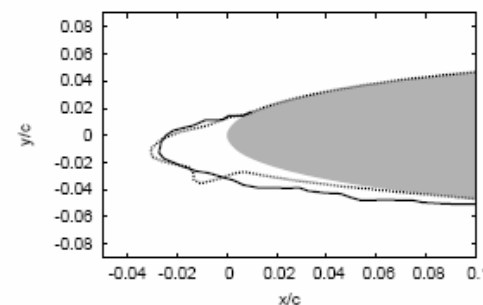
Experimental — Present Work ·····

$$T_{\infty} = 267,6 \text{ K}$$



Experimental — Present Work ·····

$$T_{\infty} = 262,1 \text{ K}$$



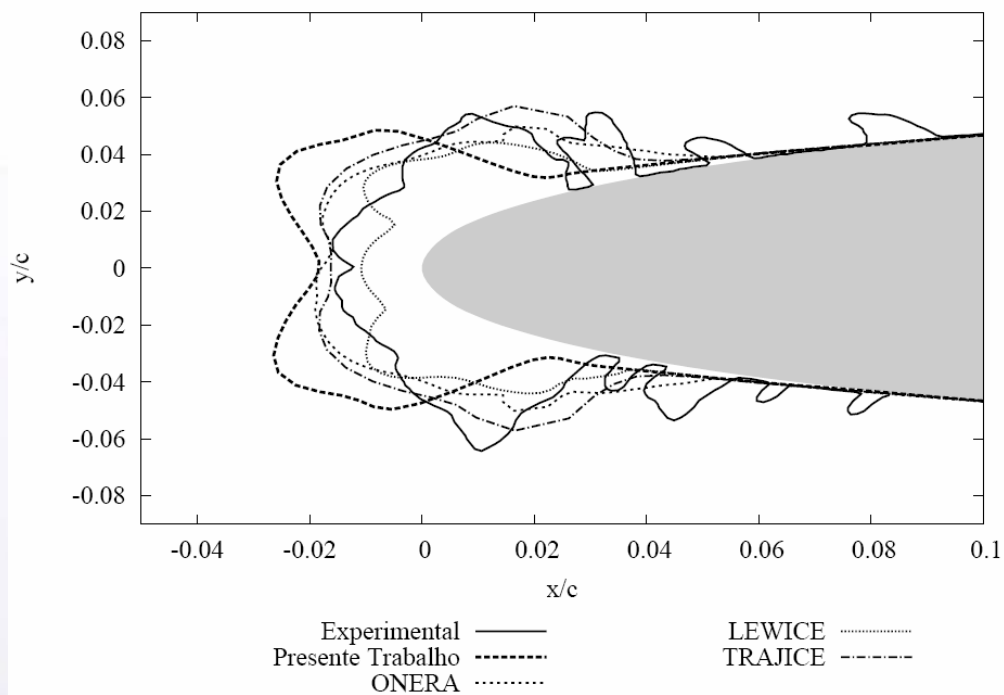
Experimental — Present Work ·····

$$T_{\infty} = 247,3 \text{ K}$$

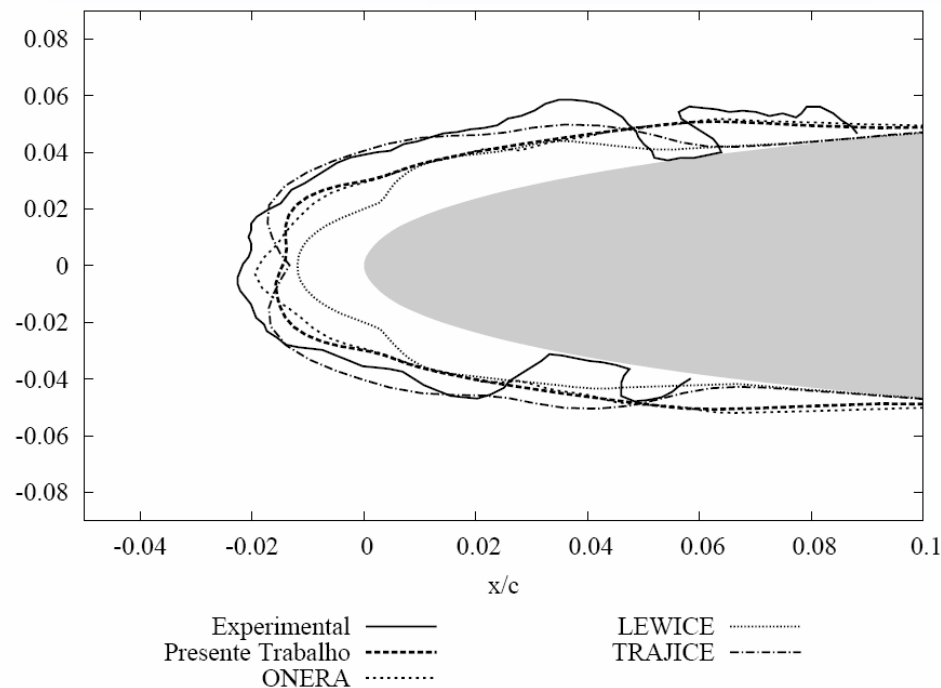
Comparison with experimental data - case F01 ( $\alpha = 4^\circ$ )



## Basic B.L. model with Abrupt Transition



case C13

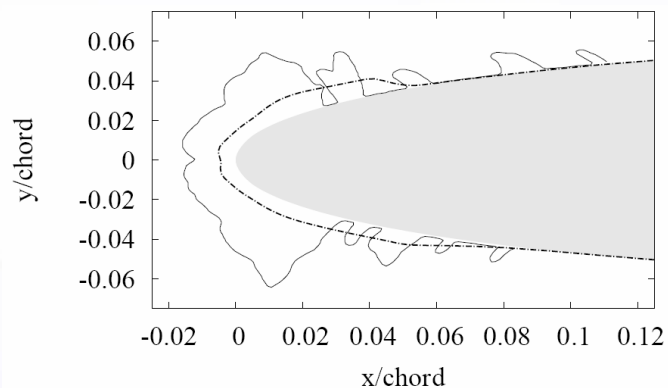


case C14

Comparison with experimental data and other codes results - case C13 and C14

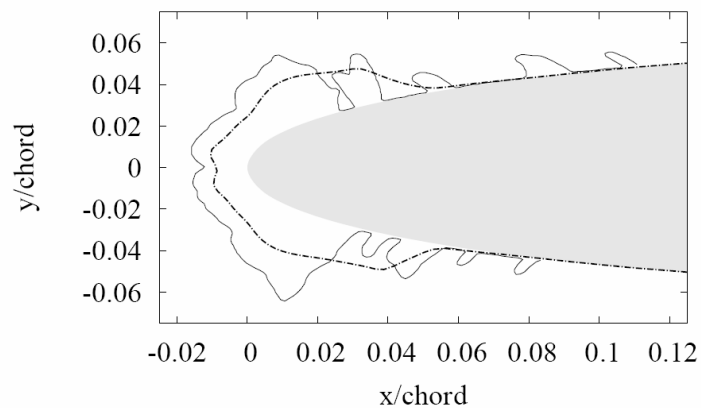


## Basic B.L. model with Smooth Transition



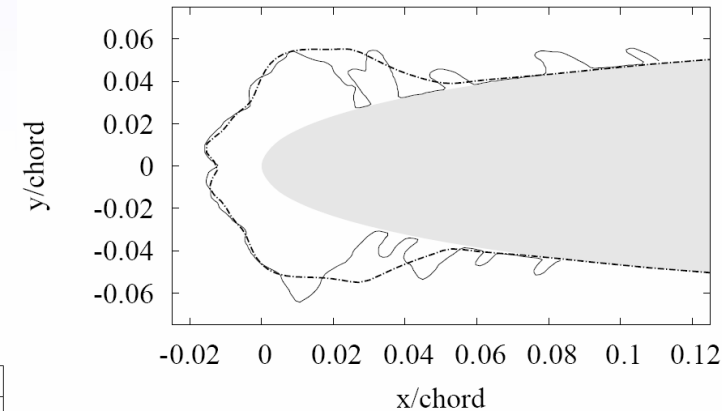
Experimental (Kind,2001) —  
Smooth-Present Simulation - - -

$t=224(\text{s})$



Experimental (Kind,2001) —  
Smooth-Present Simulation - - -

$t=448(\text{s})$



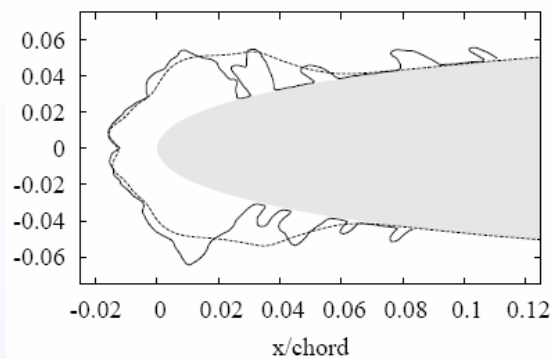
Experimental (Kind,2001) —  
Smooth-Present Simulation - - -

$t=672(\text{s})$

## Icing Growth - case C13 ( $\alpha = 0^\circ$ )

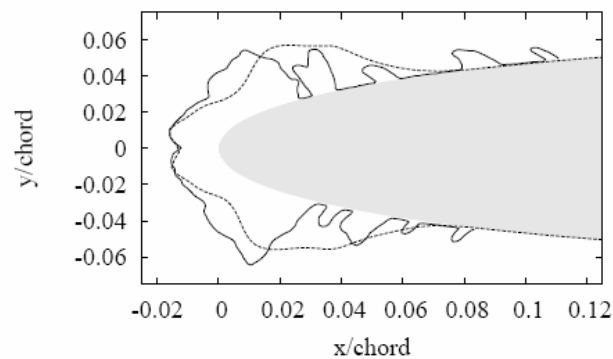


## Basic B.L. model with smooth transition



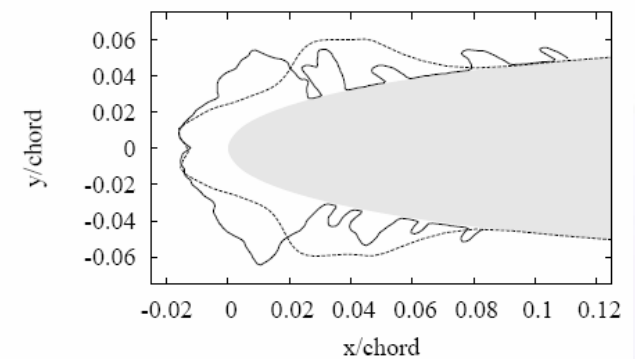
Experimental (Kind,2001) —  
Smooth-Present Simulation - - -

$$s_o/c = 0.003/-0.001$$



Experimental (Kind,2001) —  
Smooth-Present Simulation - - -

$$s_o/c = 0.013/-0.011$$



Experimental (Kind,2001) —  
Smooth-Present Simulation - - -

$$s_o/c = 0.023/-0.021$$

Transition onset : variable

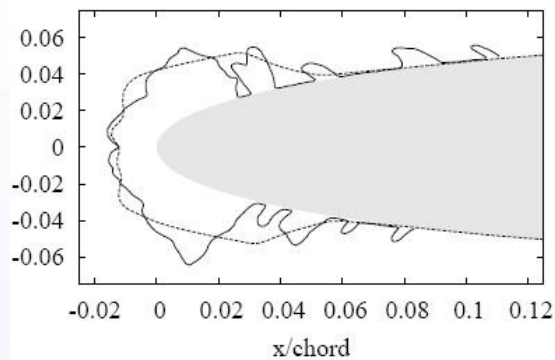
Transition length : fixed at  $l/c = 0.038 / 0.036$  (Outb/Inb)

Sand grain roughness : fixed at  $k_s = 0.125$  mm

Variation of transition onset with fixed transition length - case C13 ( $\alpha = 0^\circ$ )

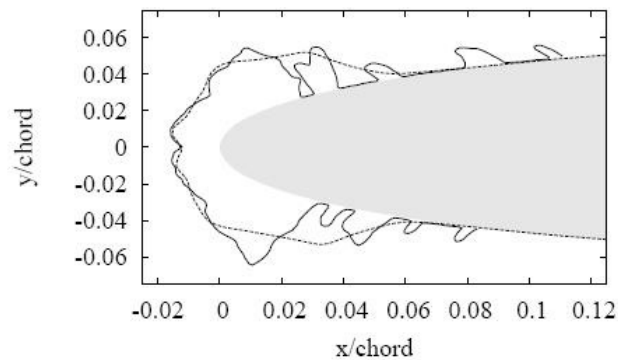


## Basic B.L. model with smooth transition



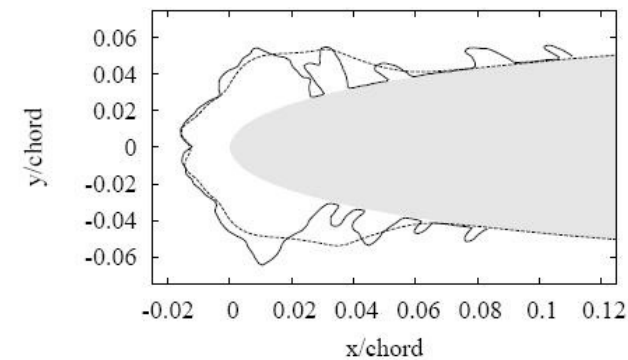
Experimental (Kind,2001) —  
Smooth-Present Simulation ·····

$s_e/c=0.021/-0.017$



Experimental (Kind,2001) —  
Smooth-Present Simulation ·····

$s_e/c=0.031/-0.027$



Experimental (Kind,2001) —  
Smooth-Present Simulation ·····

$s_e/c=0.041/-0.037$

Transition length : variable

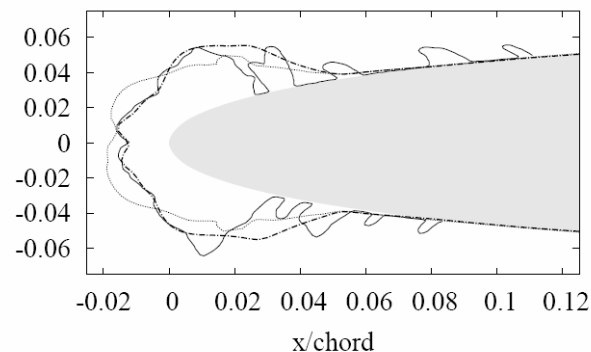
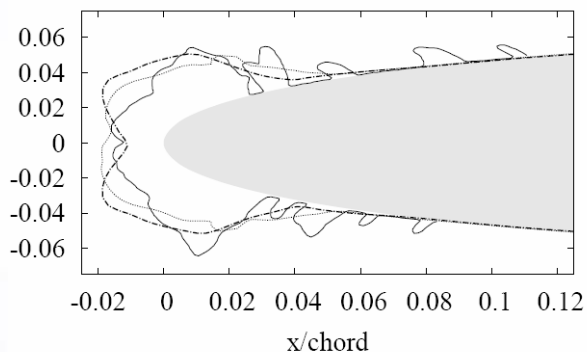
Transition onset : fixed at  $s_o/c = 0.003/-0.001$  (Outb/Inb)

Sand grain roughness : fixed at  $k_s = 0.125$  mm

### Variation of transition length with fixed transition onset - case C13 ( $\alpha = 0^\circ$ )

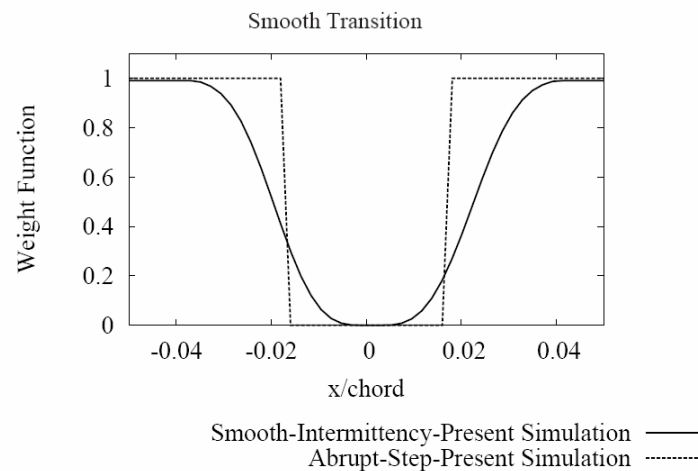
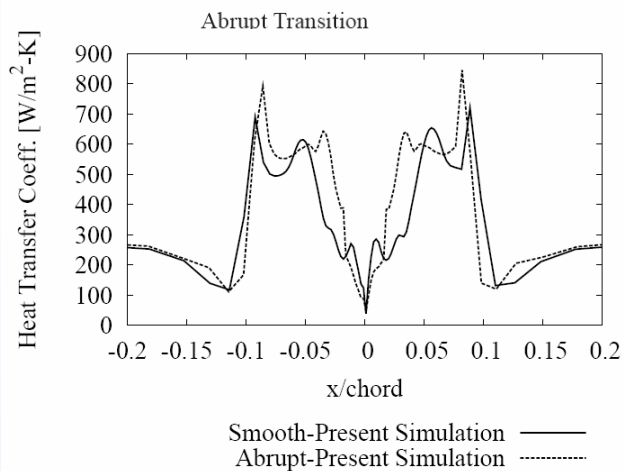


# Basic B.L. model with smooth and abrupt transition



Experimental (Kind,2001) —  
Abrupt-ONERA2D by Guffond (Kind,2001) - - -  
Abrupt-Present Simulation - - - - -

Experimental (Kind,2001) —  
Smooth-Present Simulation - - - - -  
Abrupt-ONERA2D by Guffond (Kind,2001) - - -



(a) Convective Heat Transfer Coefficient

(b) Intermittency (smooth) and Step (abrupt) Functions

## Onset and length of the transition adjusted for a fixed sand grain roughness - case C13





## Future Developments

- Modeling of transitory icing accretion on airfoils for application in electro-thermal de-icing systems
- Effects of water film roughness in the boundary layer
- Water Droplets coalescence and water film formation
- Effects of the evaporation and heating flux in the thermal boundary layer
- Development of 3D anti-icing models
- Development of scale laws to support tunnel tests of airfoils with anti-icing systems

## Published Works

- Silva, G. A. L., Silvaes, O. M., and Zerbini, E. J. G. J.,; Hefazi, H; Chen, H. H.; Kaups, K.. Differential Boundary-Layer Analysis and Runback Water Flow Model Applied to Flow Around Airfoils with Anti-ice Systems. In Proceeding of 1st AIAA Atmospheric and Space Environments, San Antonio, 2009. Reston: AIAA, 2009.
- Silva, G. A. L., Silvaes, O. M., and Zerbini, E. J. G. J., “Aircraft wing electrothermal anti-icing: Heat and mass transfer effects”. In Proceedings of Eurotherm, 5th European Thermal- Sciences Conference, Eindhoven, 2008, Eurotherm
- Silva, G. A. L., Silvaes, O. M., and Zerbini, E. J. G. J., “Differential and integral analyses of the convective heat transfer around ice protected airfoils”. In Proceedings of CHT- 08, ICHMT International Symposium on Advances in Computational Heat Transfer, Marrakesh, 2008, Ankara: ICHMT, 2008
- Silva, G. A. L., Silvaes, O. M., and Zerbini, E. J. G. J. Boundary-layers integral analysis - heated airfoils in ice conditions. In AIAA Paper 2008-0475, AIAA Aerospace Sciences Meeting and Exhibit, 46th, Reno, 2008, Reston: AIAA, 2008
- Stefanini, L. M., Silvaes, O. M., Silva, G. A. L., and Zerbini, E. J. G. J. Boundary-layers integral analysis - airfoil icing. In AIAA Paper 2008-474 (Reston, January 2007), AIAA Aerospace Sciences Meeting and Exhibit, 46th, 2008, Reno, Reston: AIAA, 2008.

## Published Works

- Silva, G. A. L., Silves, O. M., and Zerbini, E. J. G. J. Numerical simulation of airfoil thermal anti-ice operation. Part 2: Implementation and results. *Journal of Aircraft* 44, 2 (March-April 2007), 634-41.
- Stefanini, L. M., Silves, O. M., Silva, G. A. L., and Zerbini, E. J. G. J. Convective heat transfer effects in airfoil icing. In *Proceedings of COBEM 2007. Brasília, 2007, 19th International Congress of Mechanical Engineering, ABCM, 2007.*
- Silva, G. A. L., Silves, O. M., and Zerbini, E. J. G. J. . Water film breakdown and rivulets formation effects on thermal anti-ice operation simulation. In: *9th AIAA/ASME Joint Thermophysics and Heat Transfer Conference, 2006, San Francisco, Ca, EUA. Proceedings of 9th AIAA/ASME Joint Thermophysics and Heat Transfer Conference. Reston: AIAA, 2006.*
- Silva, G. A. L., Silves, O. M., and Zerbini, E. J. G. J.. Simulation of an airfoil electro-thermal anti-ice system operating in running wet regime. In: *43rd AIAA Aerospace Sciences Meeting and Exhibit, 2005, Reno, Nevada, EUA. Proceedings of 43rd AIAA Aerospace Sciences Meeting and Exhibit, Reno, Nevada, Jan. 10-13, 2005. Reston: AIAA, 2005. p. 1-11.*
- Silva, G. A. L., Silves, O. M., and Zerbini, E. J. G. J. . Airfoil anti-ice system modeling and simulation. In: *41st Aerospace Science Meeting and Exhibit, 2003, Reno. 41st Aerospace Science Meeting and Exhibit. Reston : AIAA, 2003. p. 1-11.*

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## Acknowledgments

- Fapesp - Fundação de Amparo à Pesquisa do Estado de São Paulo
- Capes - Coordenação de Aperfeiçoamento de Pessoal de Nível Superior
- Embraer - Empresa Brasileira de Aeronáutica S.A.
- CSULB - California State University, Long Beach
- USP - Universidade de São Paulo
- ATS4i - Aero-Thermal Solutions for Industry



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